

1. INTRODUCTION

The India-based Neutrino Observatory (INO) is a proposed underground facility for hosting decisive neutrino experiments. The magnetized iron calorimeter (ICAL) detector at INO with charge identification capability will study the oscillation pattern of atmospheric neutrinos. In the 1st phase it aims at precise measurement of oscillation parameters, probing neutrino mass hierarchy as well as new physics.

A brief overview of ICAL detector:

- Dimension: 48m × 16m × 14.4m (3 modules of dimensions 16m × 16m × 14.4m each)
- Mass: 50 kTon (approximately).
- Absorber: Iron plates of thickness 5.6 cm.
- Active detector volume: Resistive Plate Chamber (RPC) (2m × 2m × 8mm). The readout of the RPC is carried out by external orthogonal pick up strips (X & Y strips).
- Magnetic Field 1.4 Tesla.

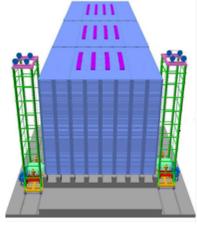


Figure 1: A sketch of the proposed INO-ICAL detector.

2. NEUTRINO INTERACTIONS IN THE DETECTOR

The atmospheric neutrinos inside the detector may interact through different processes:

- The Quasi-Elastic Charge Current (QECC) interaction events. They produce associated leptons.
- Deep Inelastic Scattering (DIS) interaction events. They produce associated leptons and hadrons.
- Resonance Interaction events. They produce single pion events.

ICAL is most sensitive to muon neutrinos. Muon gives distinct track, and hadron produces shower.

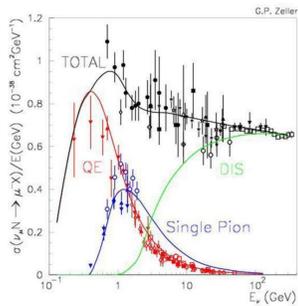


Figure 2: The energy dependence of the cross sections of different interaction processes.

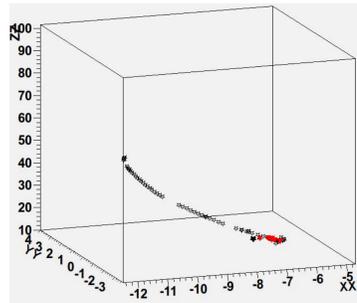


Figure 3: An DIS event in INO-ICAL detector. Black points: muon track, red ones: hadron shower.

3. THE IMPORTANCE OF HADRONIC RESPONSE OF INO-ICAL

- Measurement of neutrino energy (E_ν) and direction plays a crucial role in fulfilling the physics goals.
- The precision in reconstructing E_ν depends on how precisely the energies of muon and the hadrons are measured.
- E_μ 's are reconstructed from the track radius in the detector.
- From the hit information of the hadron shower, the hadron energy needs to be estimated.
- To reconstruct the incident neutrino direction, the information of the directions of muon and hadrons are needed.
- For hadron shower, fluctuation in energy loss is much larger than the e.m. process.
- The hadron energy resolution is affected by energy leakage and invisible energy loss mechanism.

4. THE DETECTOR SIMULATION

- Simulation Toolkit: GEANT4. Storage of output & analysis: ROOT.
- The simulation framework consists of the following:
 1. Event Generation (GEANT4 / NUANCEV3): Particles resulting from random interactions of neutrinos with matter using theoretical models are generated. The outputs are: Reaction channels, vertex information, energy and momentum of the particles.
 2. Event Simulation (GEANT4): Propagation of the particles through the detector are simulated. The outputs are: position and time of the particles at the vertex, the energy deposited and the momentum.
 3. Event digitisation (GEANT4): The detector efficiency and noise are added. The output of simulation is digitised in this step.
 4. Event reconstruction (GEANT4): Track finding and track fitting are done.
- The hadronic response of INO-ICAL are studied using both single pion events from GEANT4 and atmospheric neutrino events from NUANCE.

5. ANALYSIS OF HADRON HIT PATTERN

The hadron hit pattern:

- The hadron hit distributions in ICAL follow Vavilov distribution function, which is used to calculate the energy loss of heavy charged particles in moderately thick absorbers.
- Example : Figure 4: hit distribution for MC π^\pm at 6 GeV.

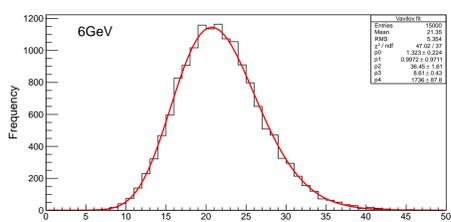


Figure 4: The hit pattern for pions at 6 GeV fitted with Vavilov distribution.

- Figure 5: The variation of average hadron hits with energy. The average hadron hit varies with energy showing saturation effects.
- In the energy region where the mean varies linearly with energy, the resolution function is $\frac{\sigma}{E} \sim \frac{\Delta E}{E}$.

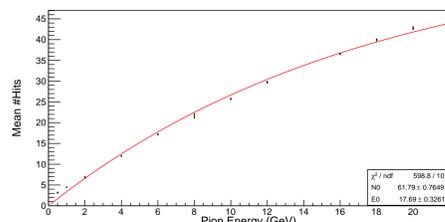


Figure 5: The variation of average hadron hits of MC π^\pm with energy.

6. THE HADRON ENERGY RESOLUTION FOR INO-ICAL

The resolution function is parametrized by

$$\frac{\sigma}{E} = \sqrt{\left(\frac{P_0}{\sqrt{E}}\right)^2 + P_1^2} \quad (1)$$

- For vertically falling Monte Carlo π^\pm events.
- For NUANCE atmospheric neutrino events.

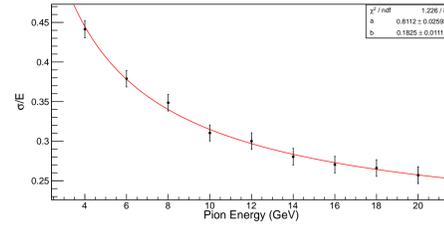


Figure 6: Hadron energy resolution for MC π^\pm events.

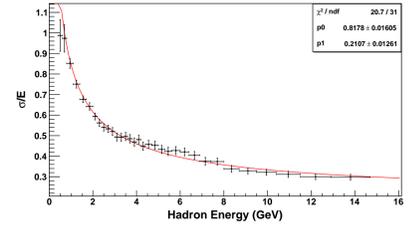


Figure 7: Hadron energy resolution for NUANCE neutrino events.

- $P_0 = 0.811 \pm 0.026$, $P_1 = 0.183 \pm 0.011$.
- Resolution (at $E = 1\text{GeV}$) $\sim (81.16 \pm 2.59)\%$.
- $P_0 = 0.818 \pm 0.016$, $P_1 = 0.211 \pm 0.013$.
- Resolution (at $E = 1\text{GeV}$) $\sim (84.45 \pm 1.58)\%$.

7. THE DIRECTION RESOLUTION OF THE HADRON SHOWER

The direction reconstruction of a hadron shower:

- The centroid of the hadron shower is formed by summing over the positions of the hits in each event.
- The direction vector of the centroid from the vertex gives the reconstructed shower direction.
- We define $\Delta\theta$ as the angle between the reconstructed shower direction and the true shower direction. The distribution of $\Delta\theta$ is fitted using the function

$$f(\Delta\theta) = A \times \Delta\theta \times \exp(-B \times \Delta\theta) \quad (2)$$

- We define the direction resolution as,

$$\sigma_\theta = \sqrt{\langle (\Delta\theta)^2 \rangle - \langle \Delta\theta \rangle^2} \quad (3)$$

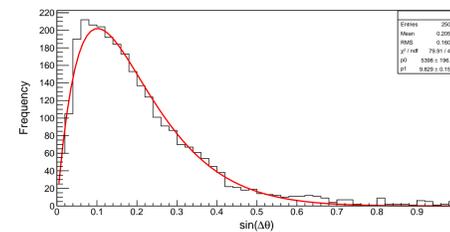


Figure 8: The $\sin(\Delta\theta)$ distribution in hadron energy bin (6.2-6.8) GeV.

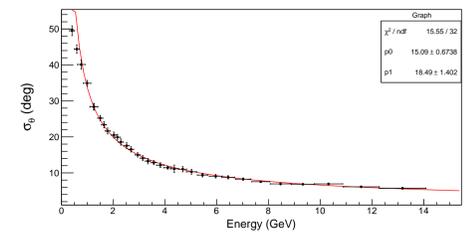


Figure 9: Direction resolution vs energy plot for NUANCE neutrino events.

- The σ_θ can be parametrized over the energy range by (Figure 9),

$$\sigma_\theta(\text{deg}) = \frac{15.09 \pm 0.67}{\sqrt{E(\text{GeV})}} + \frac{18.49 \pm 1.40}{E(\text{GeV})} \quad (4)$$

8. CALIBRATION OF HADRON ENERGY & SHOWER DIRECTION FROM HADRON HITS

- The simulated data are divided into some (reconstructed hadron direction, number of hadron hits) bins and for each bin, calibration plots are obtained for hadron energy and direction resolution.
- Examples of calibration plot: for the $\cos\theta$ bins [0,-0.2], [-0.2,-0.4], [-0.4,-0.6], [-0.6,-0.8], [-0.8,-1].

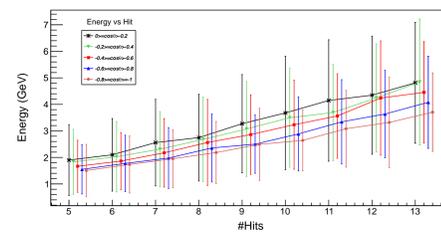


Figure 10: Calibration of Hadron Energy with Hadron Hits.

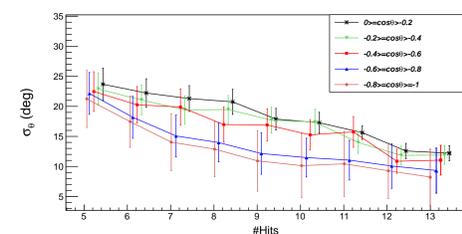


Figure 11: Calibration of hadron shower direction resolution with hadron hits.

- Using these calibration plots, the hadron energy and shower direction of an event can be estimated from the hit information.

9. CONCLUSIONS

- We have analysed the hadron energy resolution and reconstruction of direction in INO-ICAL detector both with MC pion events and hadrons shower in NUANCE neutrino events.
- The hit pattern was fitted with Vavilov pdf and the energy resolution at 1GeV is around 80 percent.
- The optimization of INO-ICAL Code for hadronic energy calibration and direction reconstruction is in progress.

10. ACKNOWLEDGEMENT

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11. REFERENCES

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