

Neutrino Phenomenology:

Highlights of oscillation results and future prospects

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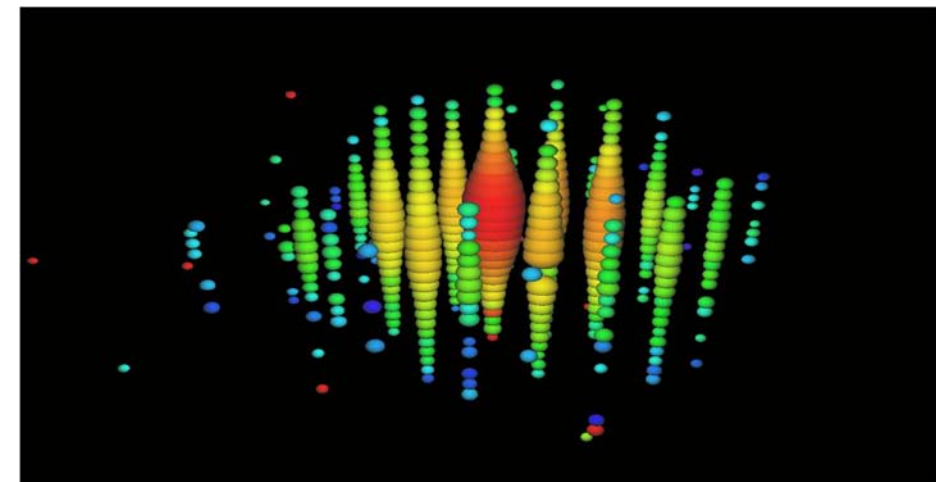
Evolution of Neutrino Physics

● The impossible dreams



● To the unreachable stars

- First detection of ultra-high energy neutrinos of extra-terrestrial origin by the ICECUBE experiment



Neutrino Oscillations

- Neutrinos are weakly interacting unlike...
- But they mix with their friends..



So much so that they get confused who they are ...



Neutrino Oscillations

• If neutrinos have mass then **Flavour states** $\nu_\alpha = \sum_i U_{\alpha i} \nu_i$ **Mass states**

• This leads to neutrino flavour oscillation in vacuum

$$P(\nu_\alpha \rightarrow \nu_\beta) = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re}[U_{\alpha i}^* U_{\alpha j} U_{\beta i} U_{\beta j}^*] \sin^2 \Delta_{ij} - 2 \sum_{i>j} \text{Im}[U_{\alpha i}^* U_{\alpha j} U_{\beta i} U_{\beta j}^*] \sin 2\Delta_{ij}$$

• $\Delta_{ij} = \Delta m_{ij}^2 L / 4E$ $\Delta m_{ij}^2 = m_i^2 - m_j^2$ $\bar{\nu} : U \rightarrow U^*$

• Interaction with matter modifies the mass, mixing and probability

• Probabilities are obtained by solving propagation equation in matter

• Depends on density profile of matter

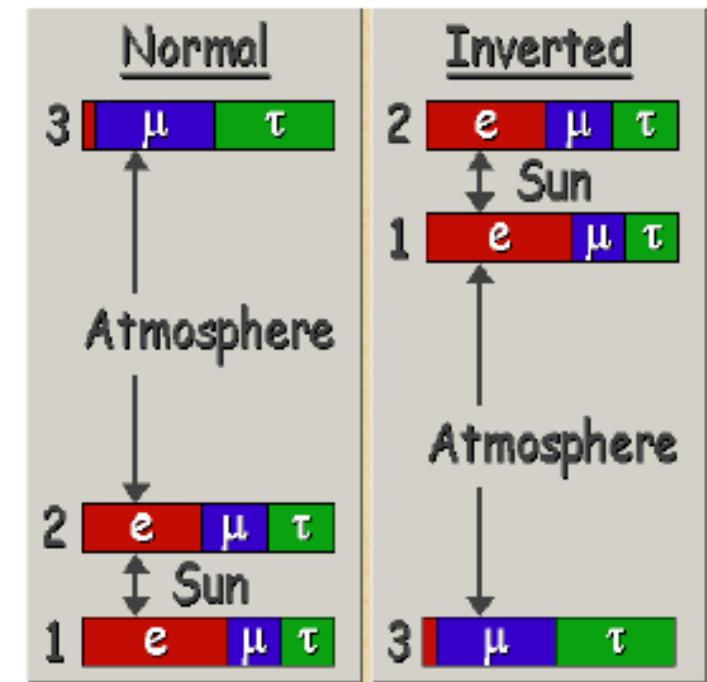
Three Neutrino Parameters

- 3 masses, 3 mixing angles and 1 Dirac +2 Majorana phases

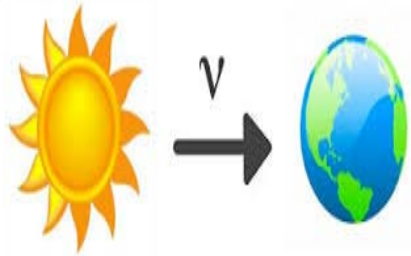
$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & & \\ & c_{23} & s_{23} \\ & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & & e^{-i\delta} s_{13} \\ & 1 & \\ -e^{i\delta} s_{13} & & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} \\ -s_{12} & c_{12} \\ & & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

$c_{12} = \cos \theta_{12}$ etc., δ CP-violating phase

- Oscillation experiments sensitive to mass squared differences $\Delta m_{21}^2 = m_2^2 - m_1^2, \Delta m_{31}^2 = m_3^2 - m_1^2$
- Two possible mass orderings
- Oscillation experiments not sensitive to Majorana phases

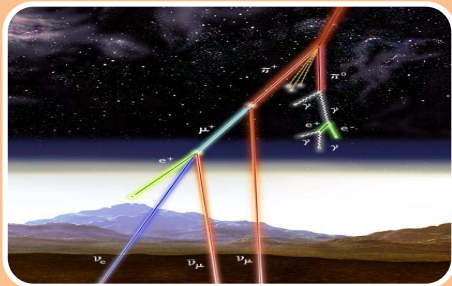


A snapshot of the oscillation experiments

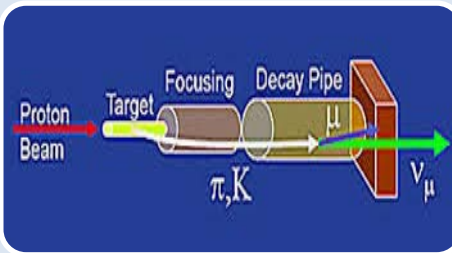


Solar Neutrinos :

Cl , Gallex/GNO/SAGE ,
SK ,SNO, Borexino



Atmospheric Neutrinos Superkamiokande



Accelerator Neutrinos K2K, MINOS ,T2K



Reactor Neutrinos

KamLAND,Palo-Varde
CHOOZ,Double-CHOOZ

Global analysis of data

$\theta_{12}, \Delta m_{21}^2, \theta_{13}$ Solar + KamLAND
 $\Delta m_{31}^2, \theta_{13}$ Reactor

$\Delta m_{31}^2, \theta_{23}, \theta_{13}, \delta_{CP}$ Atmospheric +LBL

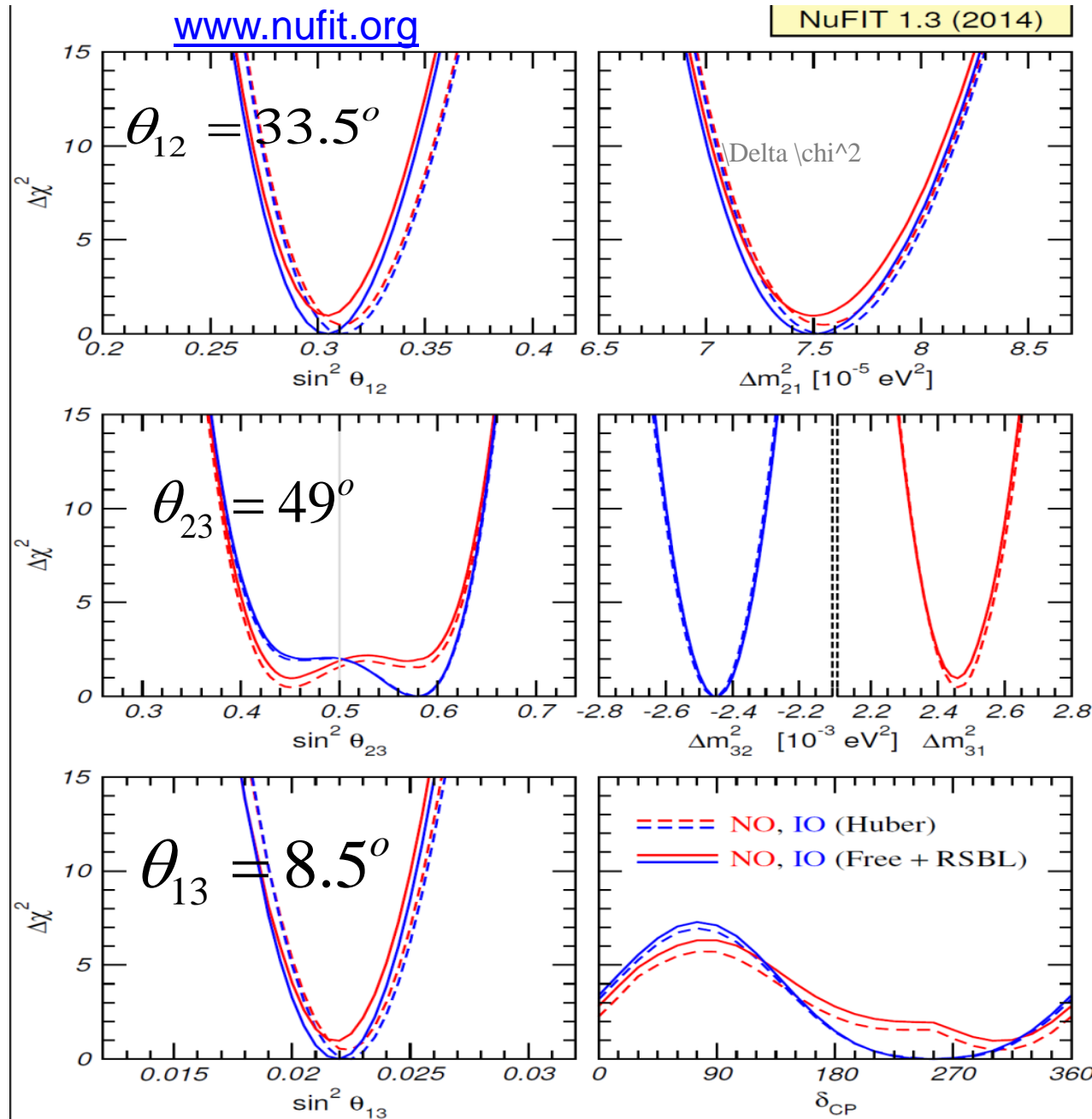
Interplay among different sectors
because of θ_{13}

New data in 2014

- New data from reactor experiments Double-Chooz, Daya-bay, Reno
- Excess around 5 MeV in RENO and Double-Chooz
- New data from ICECUBE, MINOS+ , SK4 atmospheric
- SK4 1306 day energy and zenith spectrum for solar
- T2K disappearance data

Talks by M. Schiozawa , H. Sekiya (SK), J. Haser (Double-CHOOZ, W. Wang(Daya-Bay), in ICHEP 2014

Status of oscillation parameters (post- Nu2014)

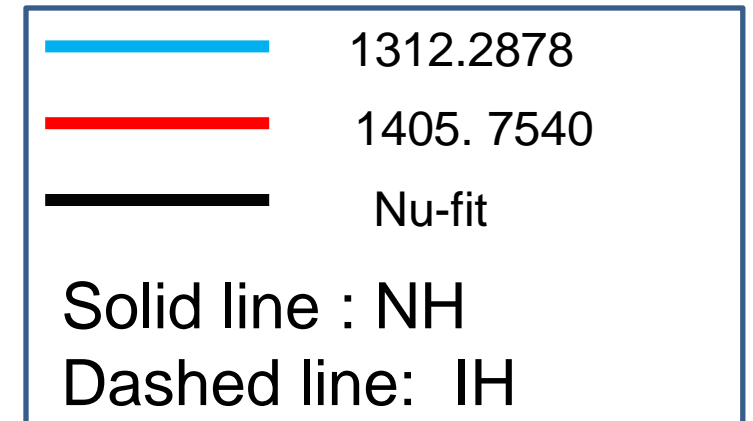
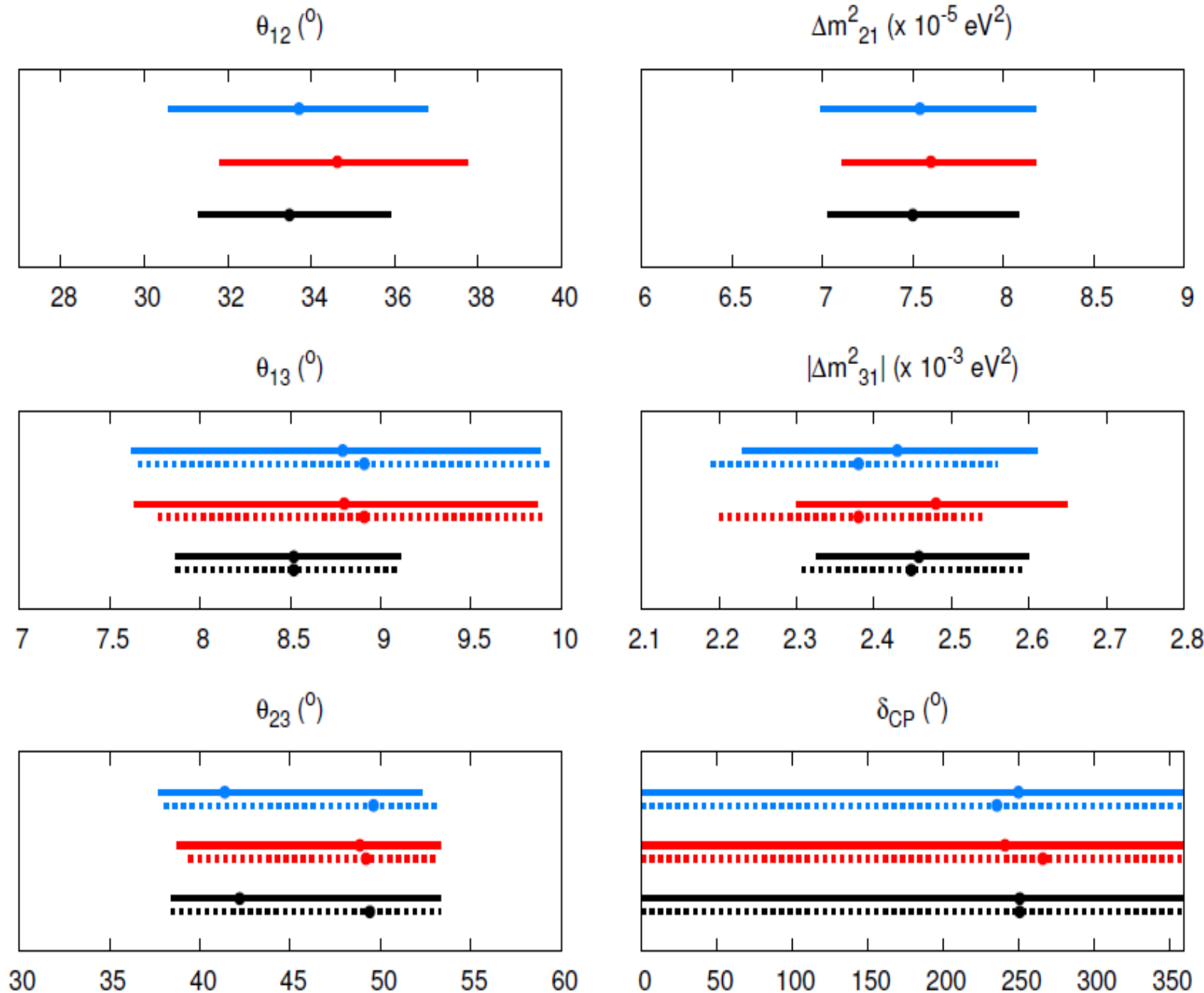


Parameter	Best fit	Precision(%)
$\sin^2 \theta_{12}$	$0.304^{+0.012}_{-0.012}$	4
$\sin^2 \theta_{23}$	$0.451^{+0.001}_{-0.001} \oplus 0.577^{+0.027}_{-0.035}$	7.5
$\sin^2 \theta_{13}$	$0.0219^{+0.0010}_{-0.0011}$	5
Δm_{21}^2 10^{-5}eV^2	$7.50^{+0.19}_{-0.17}$	2.3
Δm_{31}^2 (N) 10^{-3}eV^2	$+2.458^{+0.002}_{-0.002}$	2
Δm_{32}^2 (I) 10^{-3}eV^2	$-2.448^{+0.047}_{-0.047}$	2
$\delta_{CP} / ^\circ$	251^{+67}_{-59}	

No hierarchy sensitivity

$$\chi^2(NH) - \chi^2(IH) < 1$$

Oscillation parameters at a glance (2014)



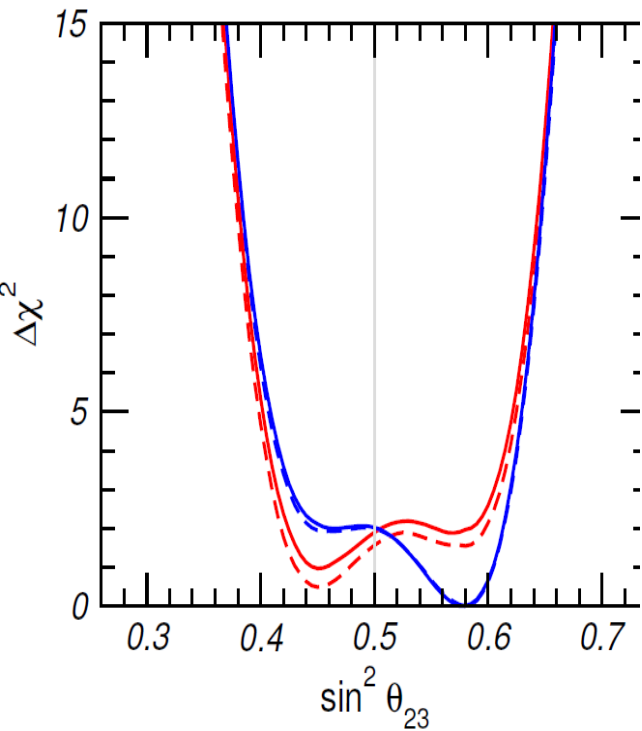
Best-fit values and 3σ range

Analysis by different groups are in agreement excepting θ_{23}

Talk by M. Tortola , ICHEP 2014

Status of θ_{23}

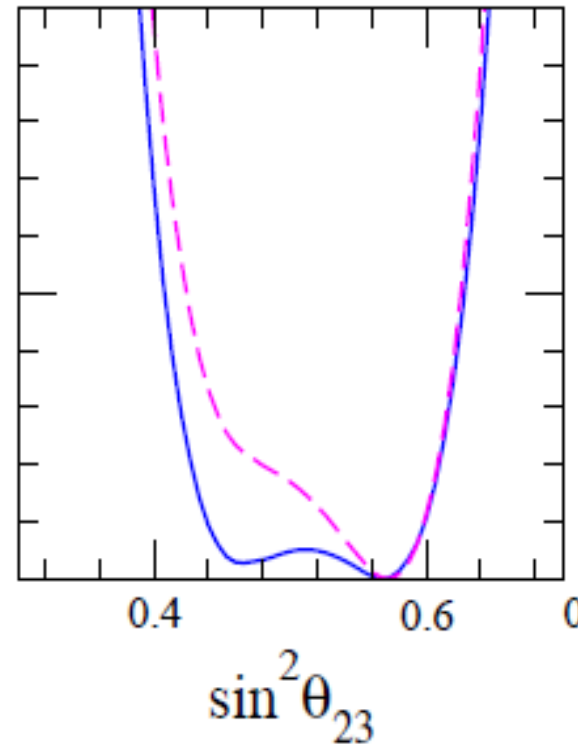
Nu-fit 2014



Global best-fit at 2nd octant and IH

NH : local best-fit at 1st octant

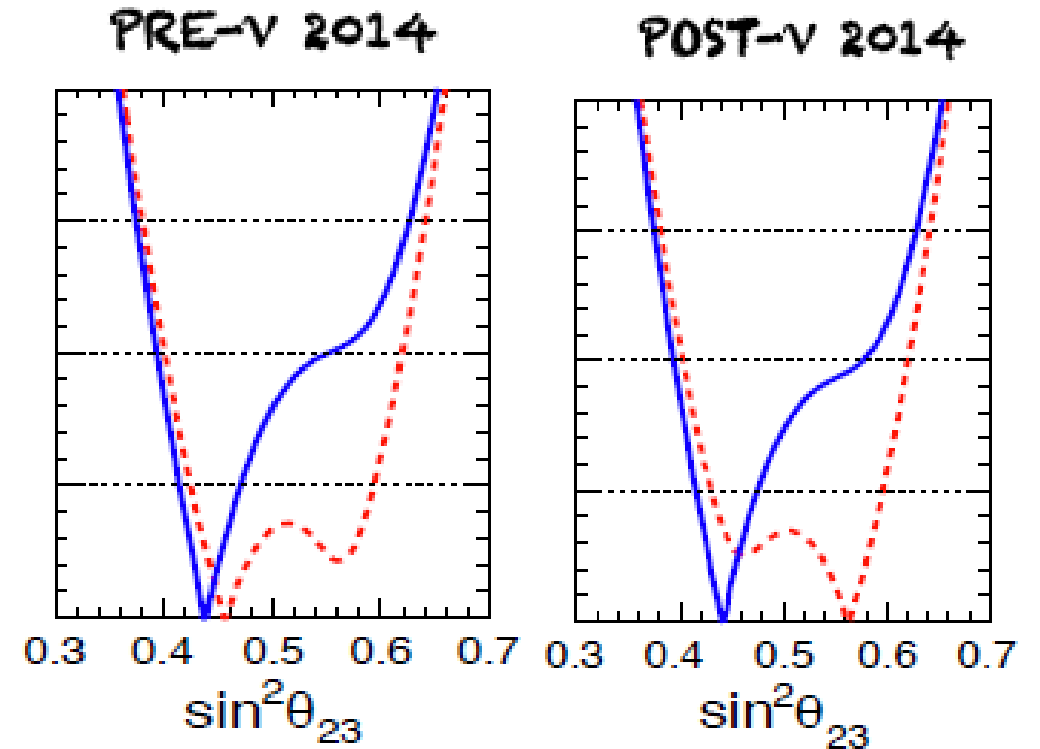
Forero et al 1405.7540



NH and IH separate fit

Best-fit at 2nd octant for both NH and IH

Capozzi et al. 1312.2878



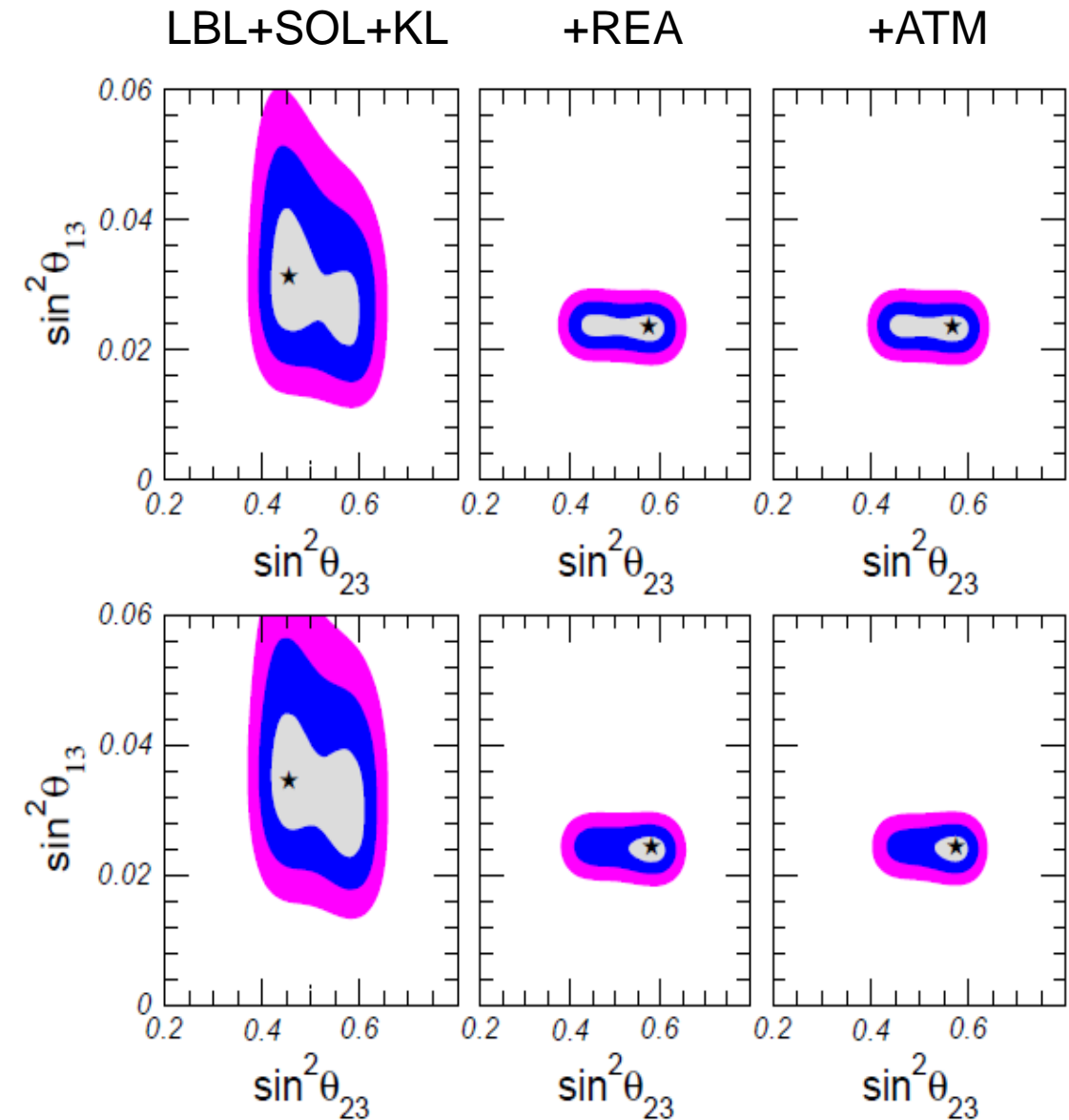
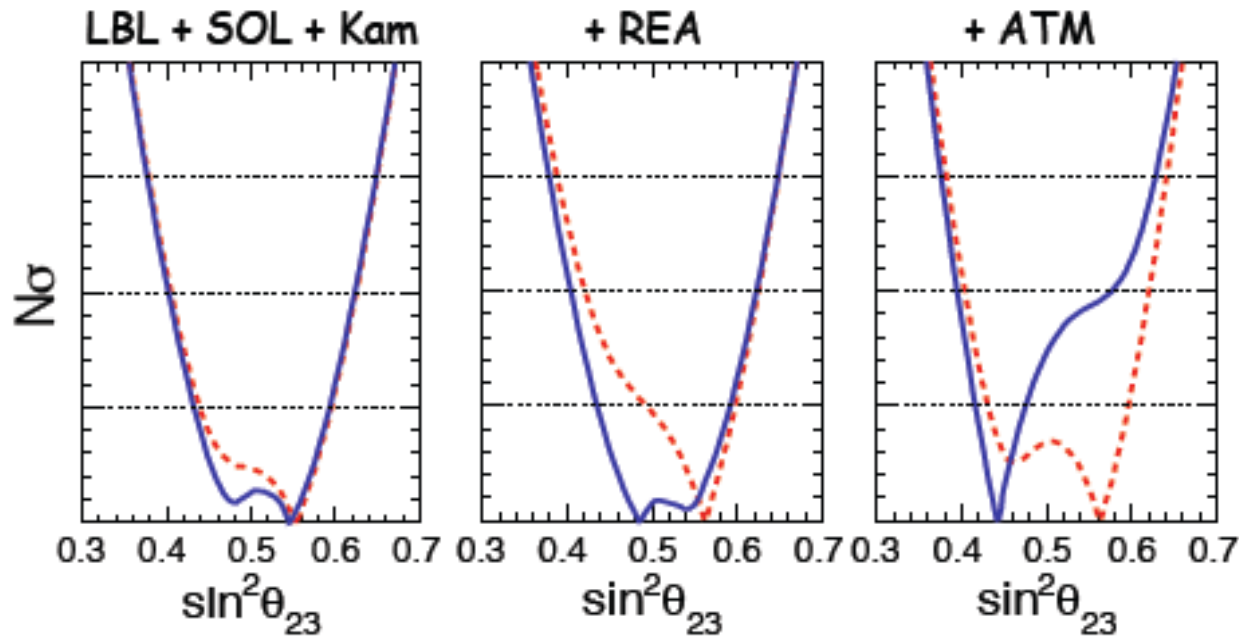
NH and IH separate fit

Best-fit in 2nd octant for IH post Neutrino 2014

Status of θ_{23} : Interplay of data

Capozzi et al. 1312.2878

Forero et al 1405.7540

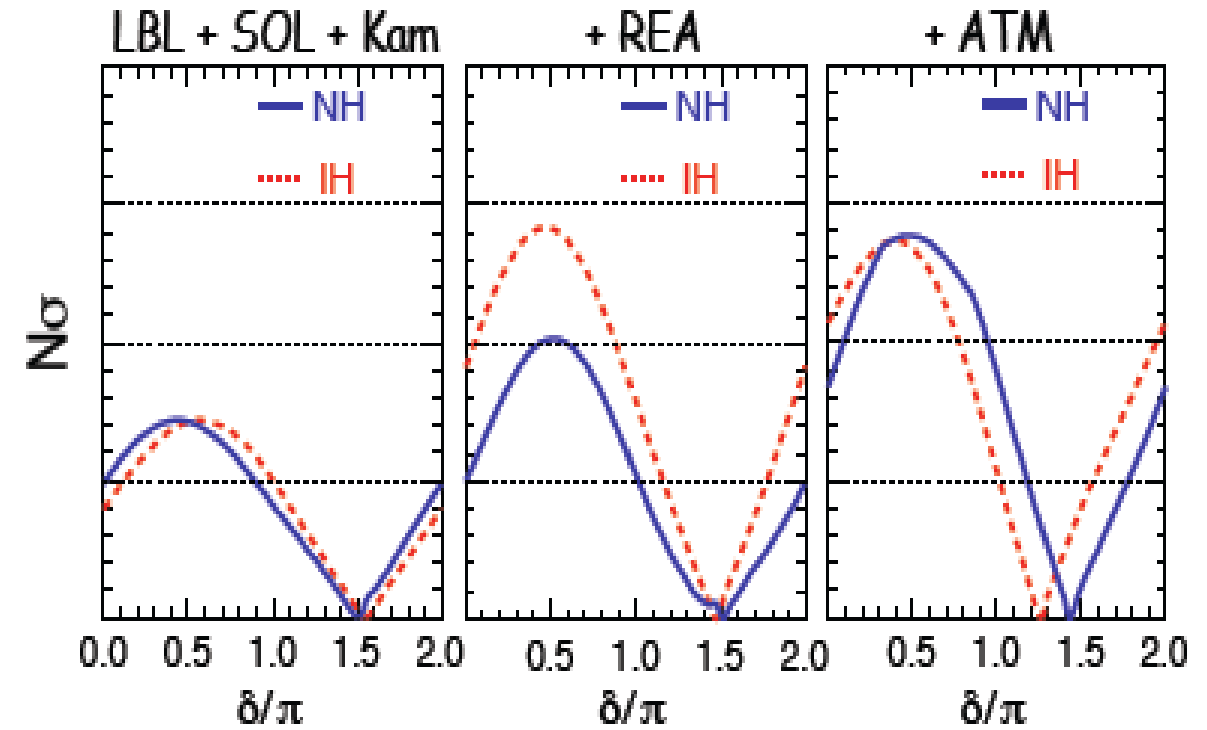
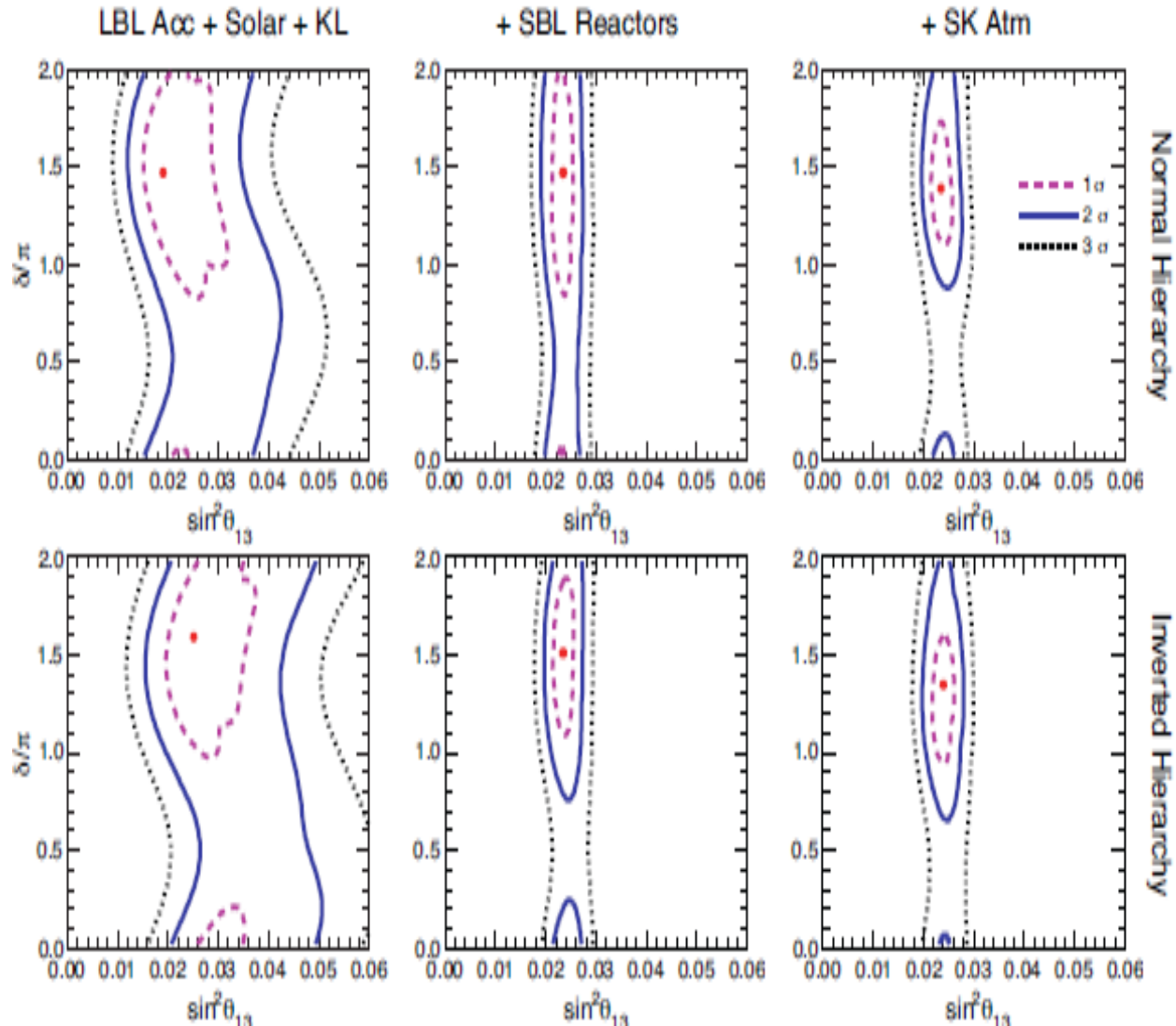


Preference for lower octant for **NH**
driven by SK atm

θ_{23} is still unstable

Status of δ_{CP} : interplay of different experiments

Capozzi et al. 1312.2878



Continued hint for $\delta_{CP} \sim 1.5\pi$
 Driven mainly by T2K appearance data
 Also SuperK atmospheric data

Progress since ICHEP – 2012

ICHEP 2012

Parameter	Best fit	Precision(%)
$\sin^2 \theta_{12}$	0.3	4
$\sin^2 \theta_{23}$	0.42	11
$\sin^2 \theta_{13}$	0.023	10
$\Delta m_{21}^2 [10^{-5} eV^2]$	7.50	2.4
$\Delta m_{31}^2 [10^{-3} eV^2]$	2.45	2.8
$ \Delta m_{32}^2 [10^{-3} eV^2]$	2.43	2.8

M.C. Gonzalez-Garcia , ICHEP 2012

ICHEP 2014

Parameter	Best fit	Precision(%)
$\sin^2 \theta_{12}$	$0.304^{+0.012}_{-0.012}$	4
$\sin^2 \theta_{23}$	$0.451^{+0.001}_{-0.001} \oplus 0.577^{+0.027}_{-0.035}$	7.5
$\sin^2 \theta_{13}$	$0.0219^{+0.0010}_{-0.0011}$	5
$\frac{\Delta m_{21}^2}{10^{-5} eV^2}$	$7.50^{+0.19}_{-0.17}$	2.3
$\frac{\Delta m_{31}^2}{10^{-3} eV^2} (N)$	$+2.458^{+0.002}_{-0.002}$	2
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$\delta_{CP} / ^\circ$	251^{+67}_{-59}	

Nu-fit 2014

Improvement in precision of θ_{13}

Improvement in precision of θ_{23}


Hint for $\delta_{CP} \sim 1.5\pi$

Precision still not as good as quark sector

The main unknowns

The absolute mass scale of neutrinos
Are neutrinos their own antiparticles

Experiments to probe this
Talk by Manfred Lindner

The neutrino mass hierarchy 
The octant of the 2-3 mixing angle
CP violation in the lepton sector
Are there sterile neutrinos

What is the mechanism of neutrino mass generation

What explains the pattern of neutrino mixing

Is low energy CP violation related to leptogenesis

Can be probed in Oscillation Experiments

Note on referencing: Some current results, initial works and ICHEP talks .Not complete (My sincere apologies) , <http://www.nu.to.infn.it/>

Future Experiments for hierarchy, octant and CP

Current Generation Superbeam Experiments

T2K : Tokai to Kamioka, 295 km . 0.76 GeV , 0.75 MW , Detector: SuperK ,taking data

NOvA : FNAL to Ash River , 810 km, 1.7 GeV, 0.7 MW, 14 kt T ASD detector, commissioning

Next generation Superbeam experiments

T2HK: JPARC to Kamioka, detector: HyperK, 1.6 Mw

LBNO : CERN to Physalami , 2290 km, 0.77MW, Detector: 24 kt LArTPC

LBNE : FNAL-LEAD , 1300km, 0.7 MW, Detector ,Detector: 34 kt LiqArTPC

ESS: European Spallation source Linac , configurations under study , 540 km, 2 GeV

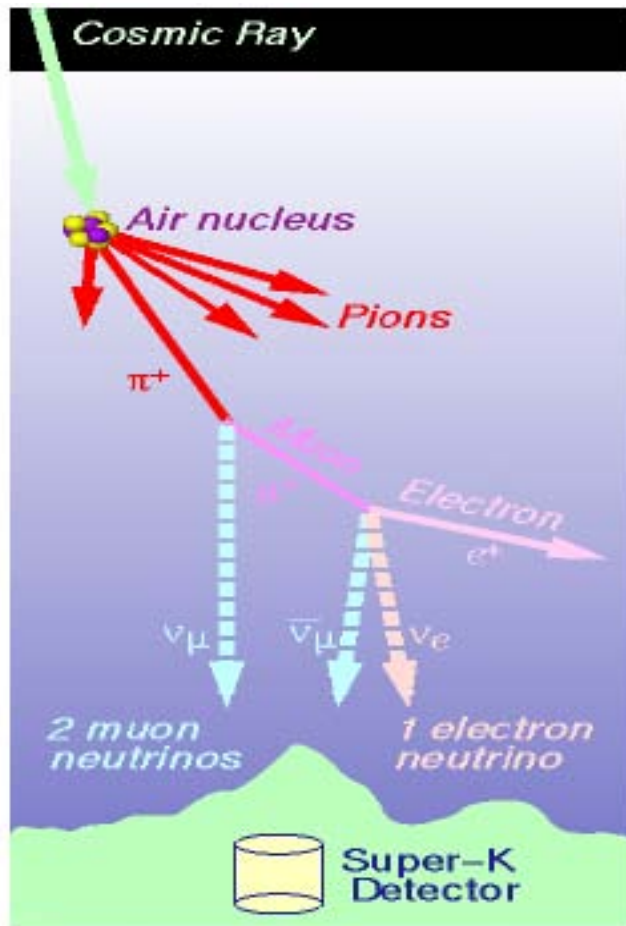
Proton decay at rest experiments

DAE δ DALUS : low energy, low distance (50 MeV, 20 km)

Reactor Experiments

JUNO (China), RENO50 (Korea) , reactor neutrinos, 50 km

Future Atmospheric Neutrino Experiments



Atmospheric neutrinos
Provide a broad L/E band

- **Magnetized Iron Detector (Prototype: INO)**
 - 50 - 100 kT
 - Excellent Muon energy measurement, direction reconstruction and charge discrimination capability
 - Can determine the neutrino energy through Hadron shower reconstruction
- **Megaton Water Cerenkov Detector (HK, MEMPHYS)**
 - Large volume (\sim Mega Ton)
 - SK-type detector with no charge ID
 - Both electron and muon events can be used
- **Liquid Argon detector (ICARUS)** ➤ Time projection chamber
 - Both electron and muon events can be used, charge ID for both?
- **(IceCube, PINGU)**
 - Huge Volume (Multi-Mton)

The survival and oscillation probabilities

In matter of constant density the survival and conversion probabilities

$$P_{\mu\mu} = 1 - \sin^2 2\theta_{23} \sin^2 \Delta + \text{sub leading terms}$$

Cerverra et al., Kimura et al .

Freund et al

Akhmedov et al ,

Talk by Yasuda, ICHEP 2014

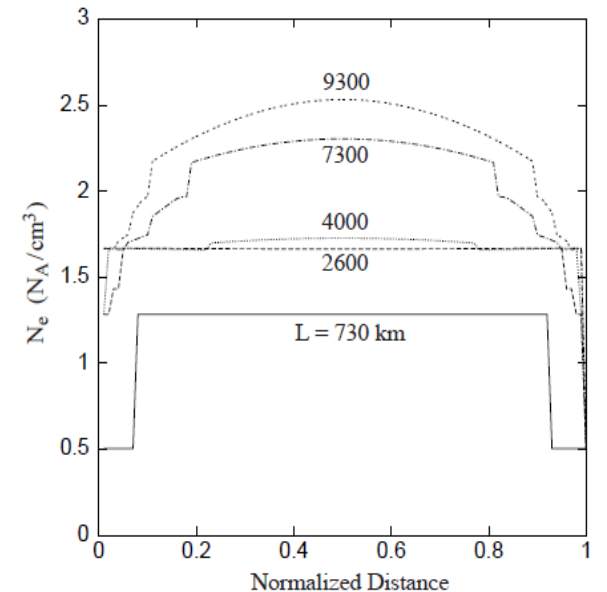
$$P_{\mu e} \simeq \sin^2 \theta_{23} \sin^2 2\theta_{13} \frac{\sin^2(\hat{A} - 1)\Delta}{(\hat{A} - 1)^2}$$

$$\Delta = \Delta m_{31}^2 L / 4E$$

$$\alpha = \Delta m_{21}^2 / \Delta m_{31}^2$$

$$+ \alpha \sin 2\theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos(\Delta + \delta_{CP}) \frac{\sin(\hat{A} - 1)\Delta \sin(\hat{A}\Delta)}{(\hat{A} - 1) \hat{A}}$$

$$+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2(\hat{A}\Delta)}{\hat{A}^2}$$



Expanded in small parameters α and $\sin^2 \theta_{13}$

Also Asano & Minakata, 2011, Agarwalla et al. 2013

$$\hat{A} = \pm 2\sqrt{2}G_F n_e E / \Delta m_{31}^2 \implies \text{Changes sign with } \text{sgn}(\Delta m_{31}^2) \implies \text{Hierarchy sensitivity}$$

+ for neutrinos

- for antineutrinos

$$P_{\mu e}(\Delta, \delta_{CP}) = P_{\mu e}(-\Delta, \delta'_{CP}) \implies \text{Hierarchy } -\delta_{CP} \text{ degeneracy}$$

Minakata, Nunokawa (2001)

Hierarchy sensitivity: T2K/NOVA

Median Sensitivity using Asimov data set (no fluctuations)

$$\Delta\chi^2 = \chi^2(NH) - \chi^2(IH)$$

Simulated Exptl data

Theory Marginalized over relevant parameters

For statistical issues see Talk by M. Blennow ICHEP 2014

For true NH ($-180^\circ < \delta_{CP} < 0$) is favourable

Degeneracy for NH +90 & IH -90

NH-IH, True(θ_{13}, θ_{23})=($9.21^0, 39^0$)

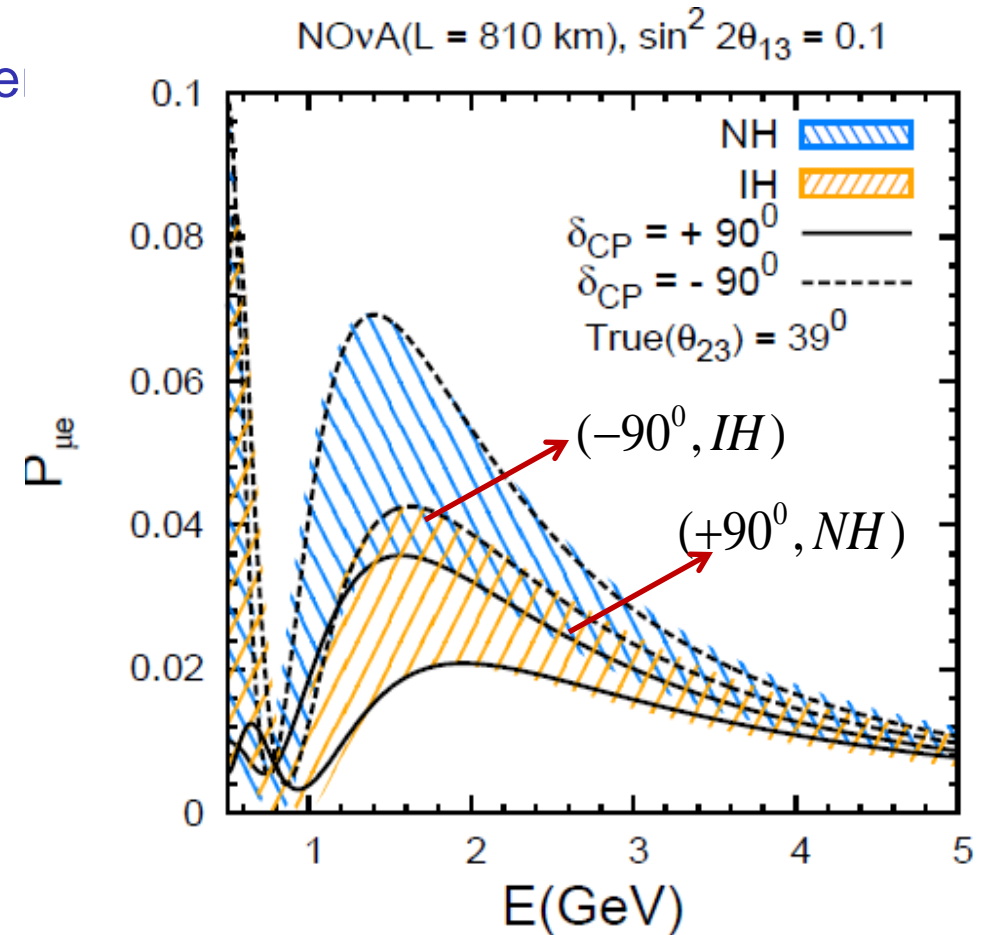
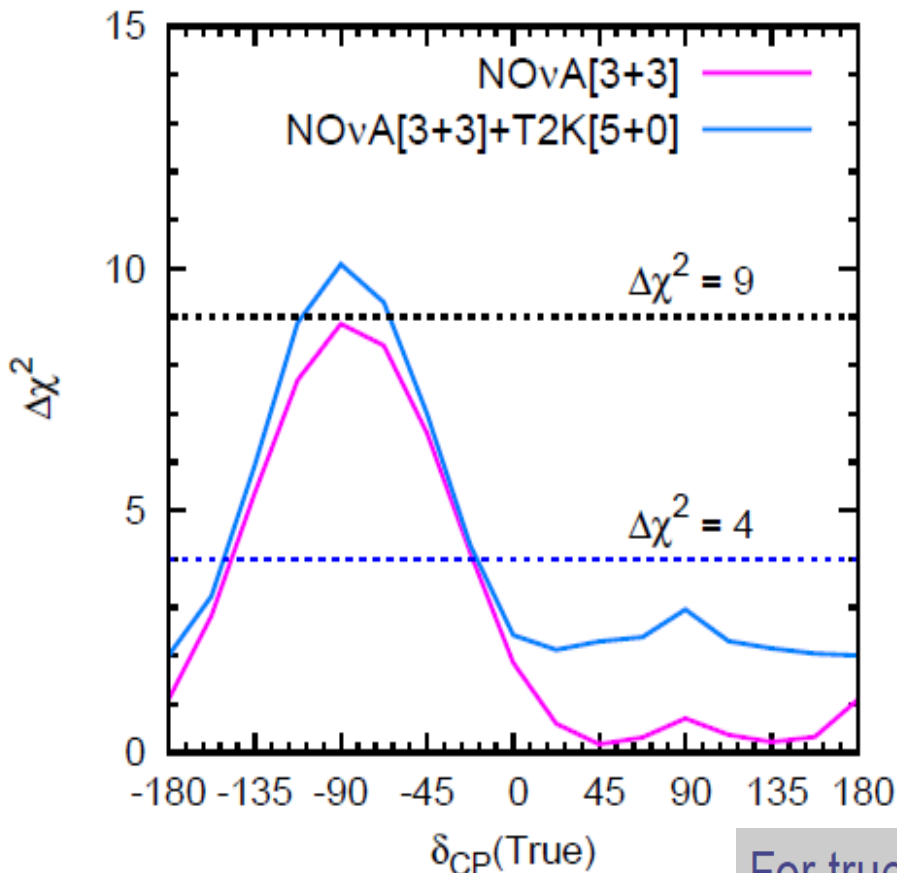
GLOBES (Huber, Kopp, Lindner, Rolinec, Winter)

T2K total pot 7.8×10^{21}

Synergy between T2K and NOvA

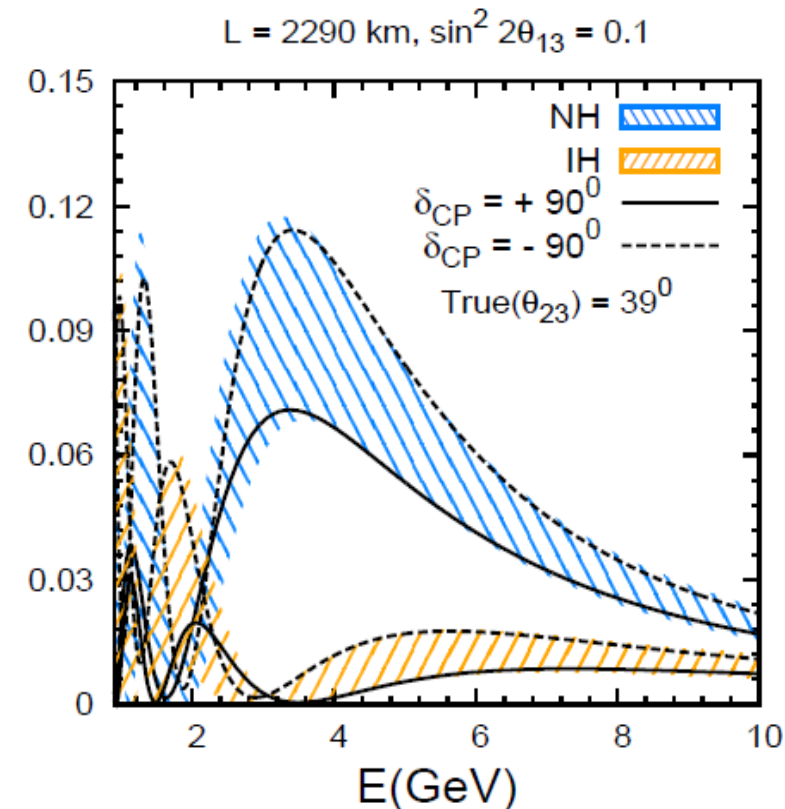
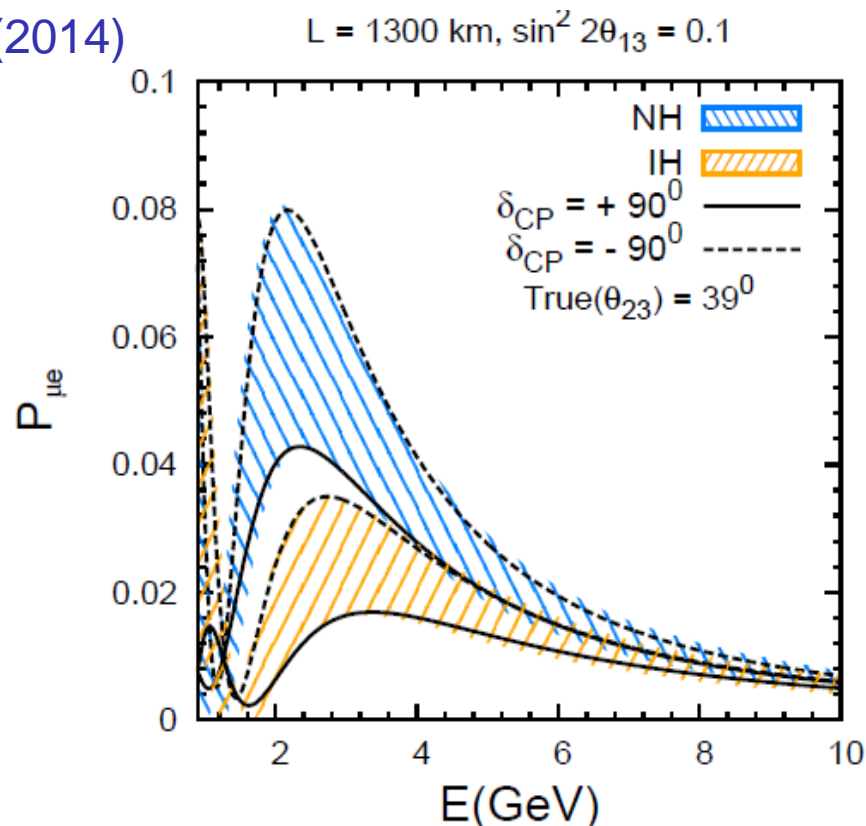
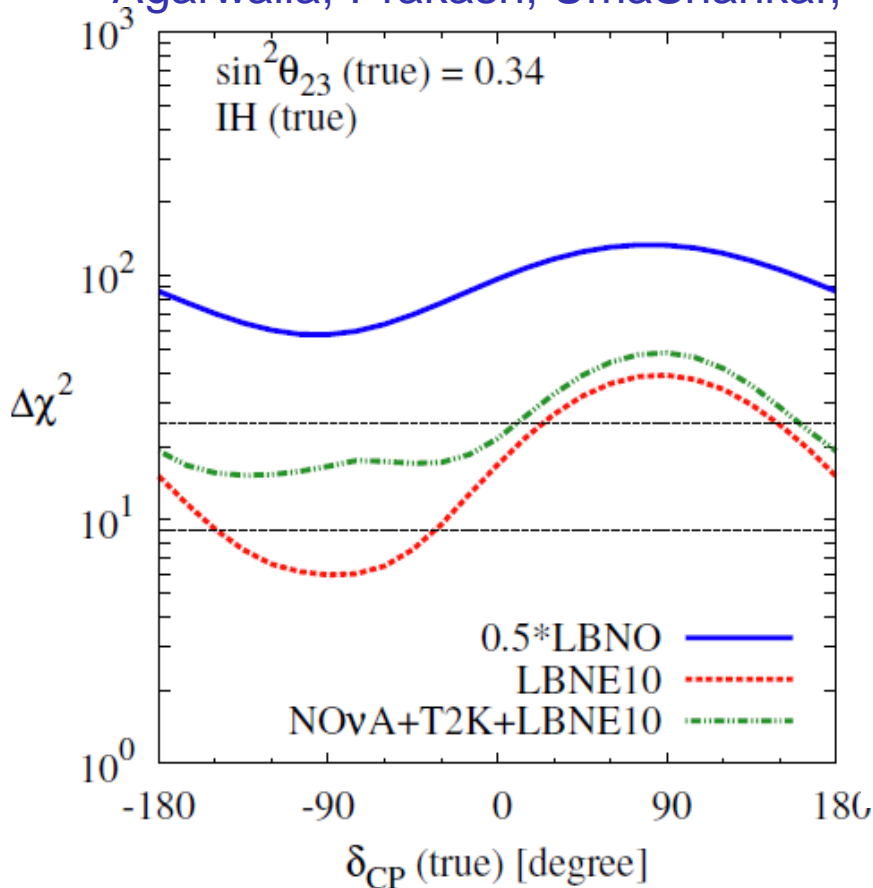
Agarwalla, Prakash, Raut, Umasankar (2012)

For true IH ($0 < \delta_{CP} < 180^\circ$) is favourable



Hierarchy Sensitivity: LBNE/LBNO

Agarwalla, Prakash, UmaShankar, (2014)



LBNE + T2K + NOvA $> 3\sigma$ for all δ_{CP}

LBNO close to 7σ for all δ_{CP}

Increased hierarchy sensitivity due to enhanced matter effects

2290 km close to Bi-Magic baseline

Talks by Z. Djurcic (LBNE), V. Galymov (LBNO) ICHEP 2014

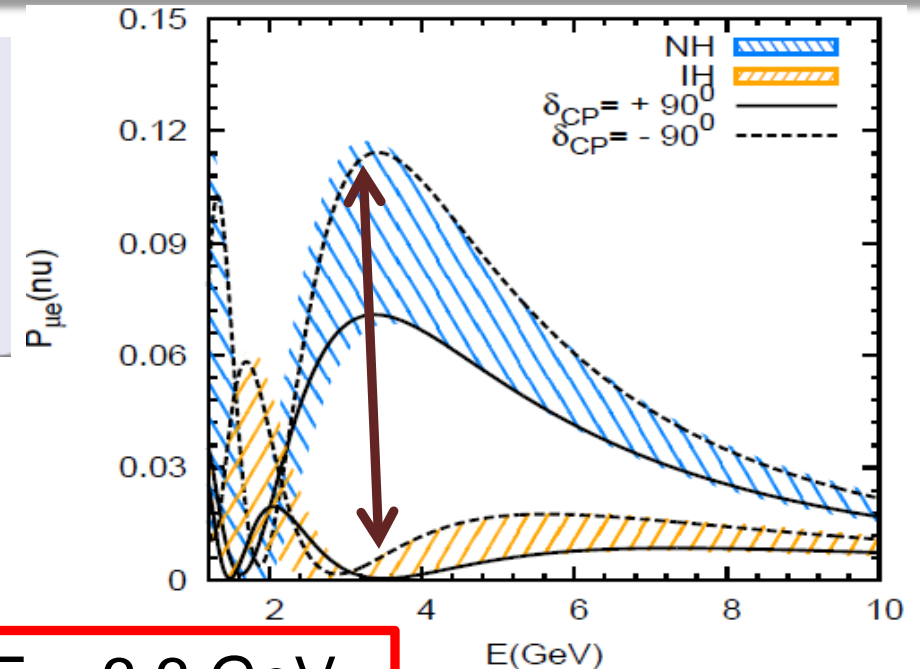
LAGUNA-LBN01312.6580, LBNE 1307.7335

Hierarchy Sensitivity: The Bi-magic baseline

$$P_{e\mu} \simeq \sin^2 \theta_{23} \sin^2 2\theta_{13} \frac{\sin^2 (1-\hat{A})\Delta}{(1-A)^2} + \alpha \sin 2\theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos(\hat{A}\Delta - \delta_{CP}) \frac{\sin(\hat{A}\Delta) \sin(1-\hat{A})\Delta}{\hat{A}(1-\hat{A})} + \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2(\hat{A}\Delta)}{\hat{A}^2}$$

Bi-magic Condition $\frac{\sin(1-\hat{A}\Delta)}{(1-\hat{A})} = 0$

Depends on hierarchy



Raut, Singh, Umasankar, 2009

IH-NoCP
 $(1 + |\hat{A}|) \cdot |\Delta| = n\pi, n > 0$

NH-max
 $(1 - |\hat{A}|) \cdot |\Delta| = (m - \frac{1}{2})\pi$



$L = 2540 \text{ km}, E = 3.3 \text{ GeV}$
 Minima for IH, CP for NH

NH-NoCP
 $(1 - |\hat{A}|) \cdot |\Delta| = n\pi, n \neq 0$

IH-max
 $(1 + |\hat{A}|) \cdot |\Delta| = (m - \frac{1}{2})\pi$



$L = 2540 \text{ km}, E = 1.9 \text{ GeV}$
 Minima for NH, CP for IH

Dighe, Goswami, Ray, 2010

Recall Magic baseline $\frac{\sin \hat{A}\Delta}{A} = 0$

$L = 7500 \text{ km}$ for both NH and IH \rightarrow no CP sensitivity

Barger, Marfatia, Whisnant 2001, Huber, Winter 2003

Resonant matter effect at large baselines

● Atmospheric neutrinos cover large distances in matter \implies Broad L/E band

● Can encounter resonance $\Delta m_{31}^2 \cos 2\theta_{13} = 2\sqrt{2}G_F n_e E$

$$\begin{aligned} \Delta m_{31}^2 &= 2.5 \times 10^{-3} \text{ eV}^2 \\ \rho_{av} &= 4.1 \text{ gm/cc} \\ E_{res} &= 7.5 \text{ GeV} \end{aligned}$$

$$\tan 2\theta_{13}^m = \frac{\Delta m_{31}^2 \sin 2\theta_{13}}{\Delta m_{31}^2 \cos 2\theta_{13} \pm 2\sqrt{2}G_F n_e E}$$

Agarwalla, Choubey, Raychaudhuri, 2006

● For $\Delta m_{31}^2 > 0$ resonance in neutrinos

● For $\Delta m_{31}^2 < 0$ resonance in antineutrinos

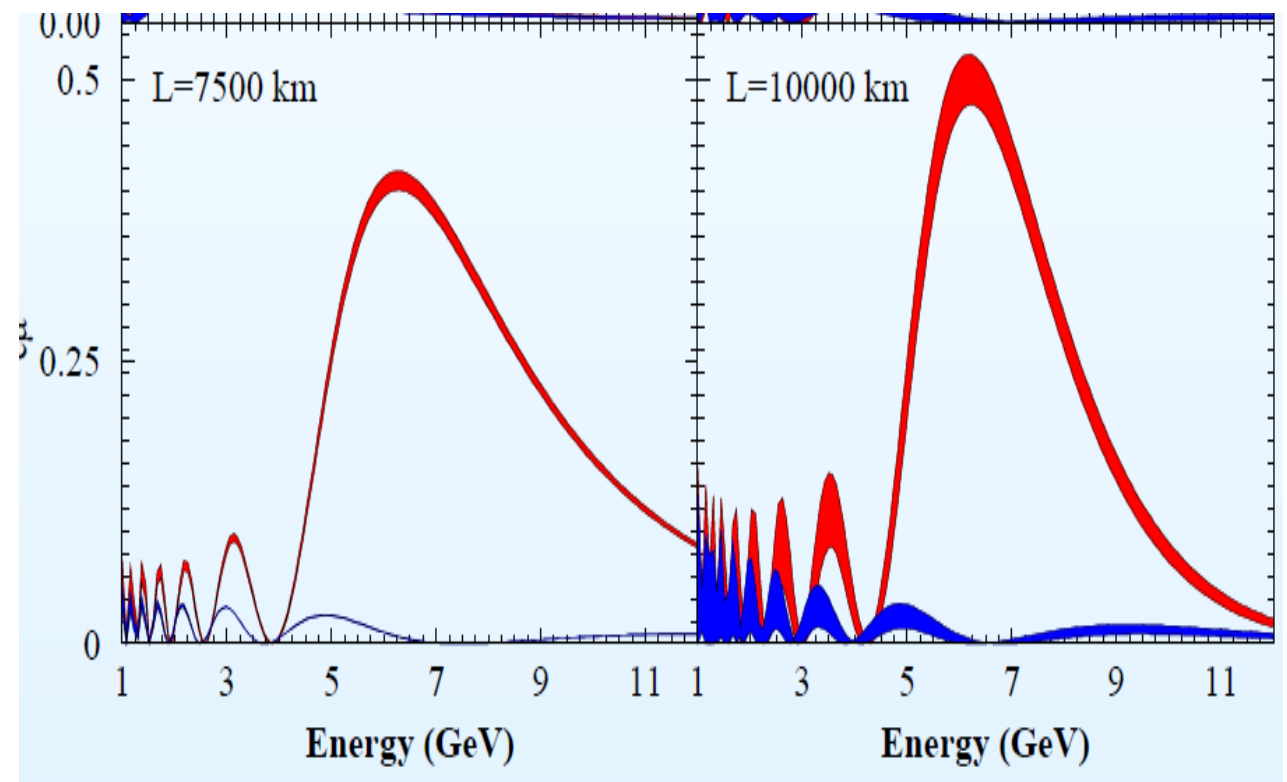


● Hierarchy Sensitivity \implies Depends on θ_{13}

● Large θ_{13} \implies Good news

● Detector with charge id important

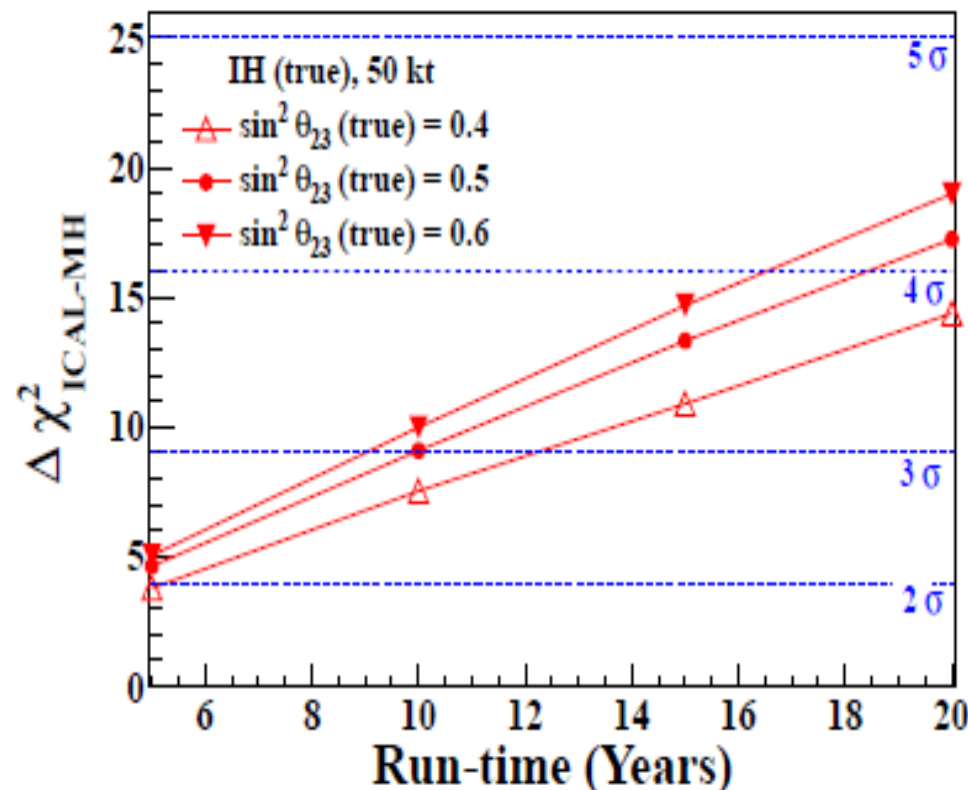
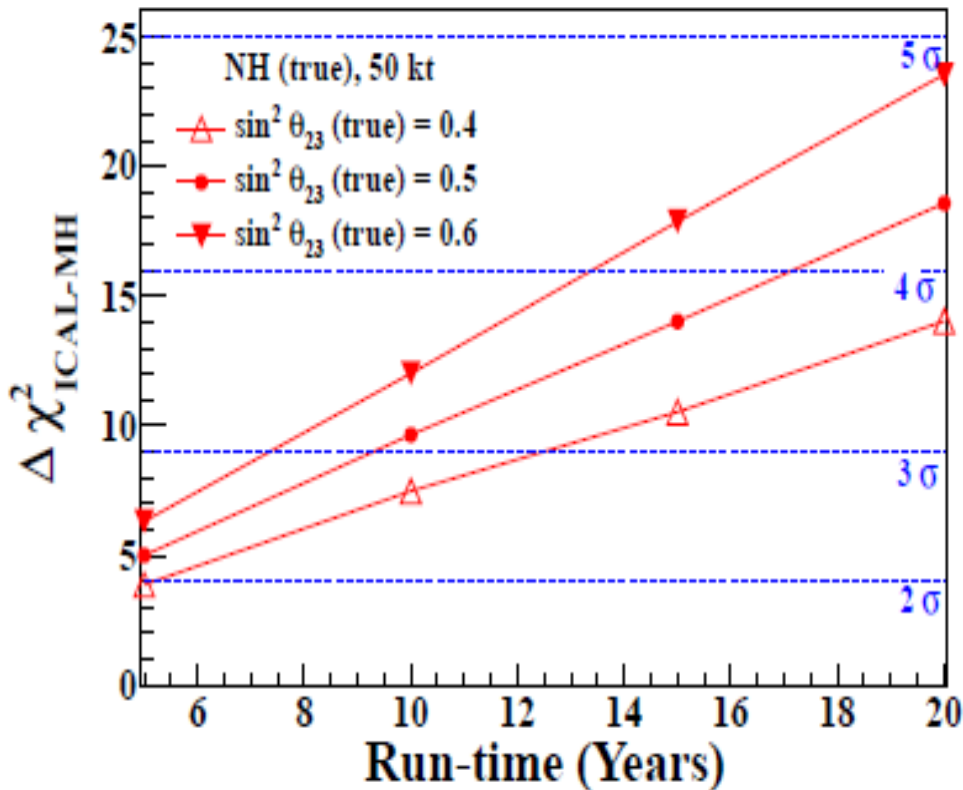
● Hierarchy - δ_{CP} degeneracy absent



Wofenstein,'78 Barger et al,'80 , Mikheyev,Smirnov'86

Hierarchy Sensitivity : Atmospheric Neutrinos (INO)

- Incorporation of Hadron information : event by event analysis in $E_\mu, \cos \theta_\mu, E_{had}$
- Improves the hierarchy sensitivity significantly : 40 % increase in χ^2



3D analysis with Information on hadron energy

Devi, Thakore, Agarwalla Dighe (2014)

Talk by Agarwalla, ICHEP 2014

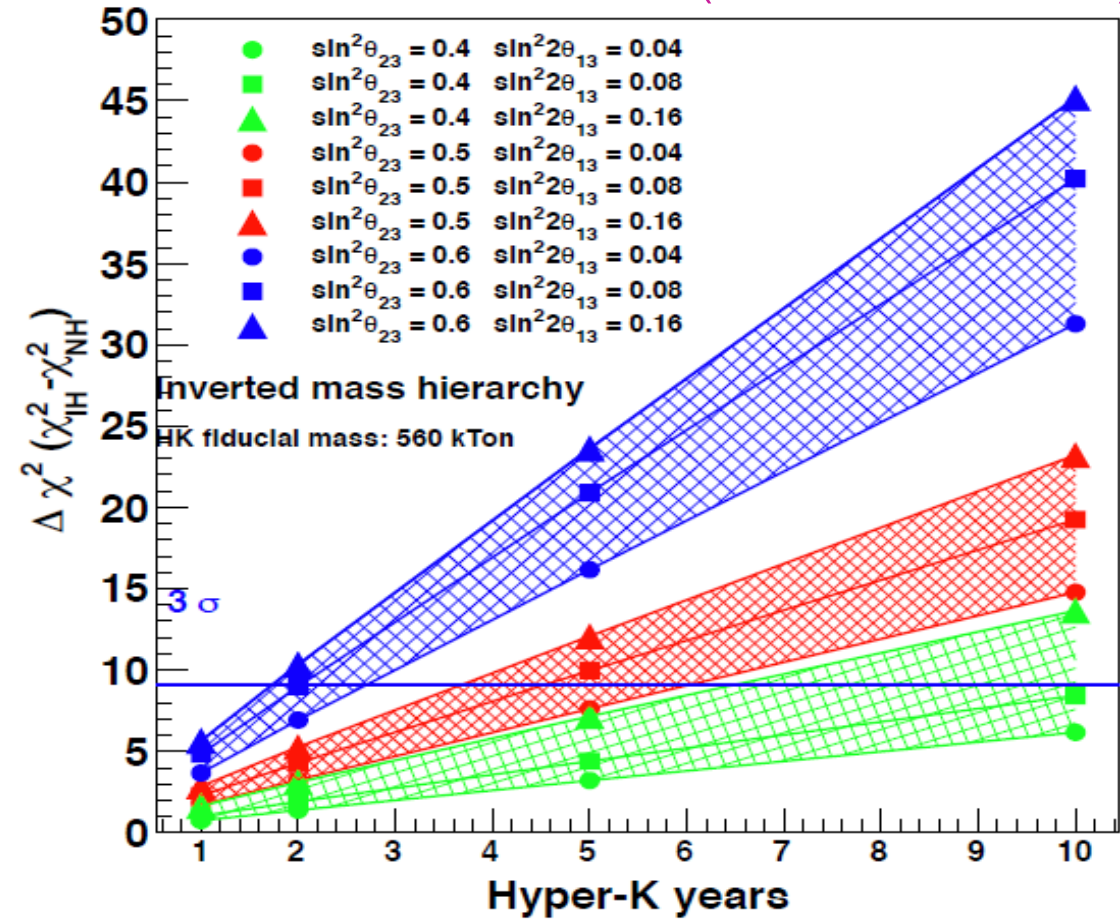
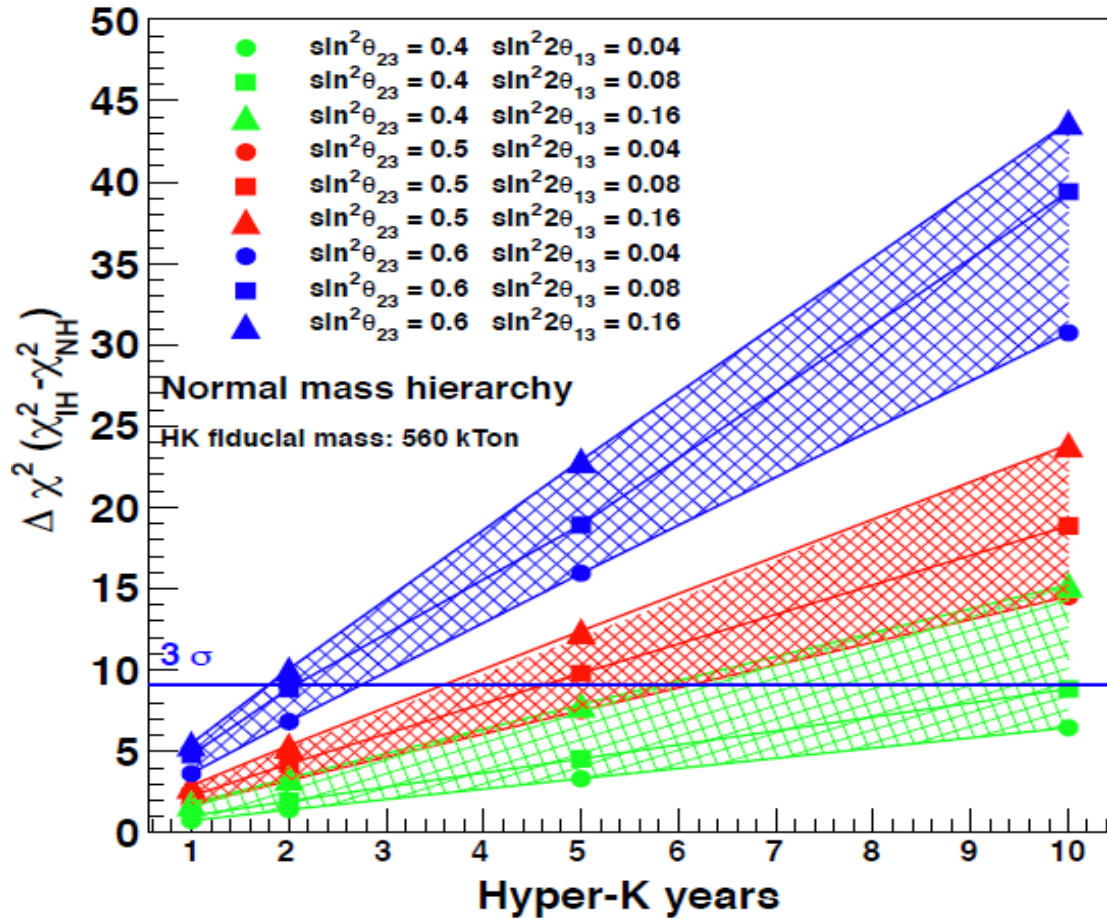
3σ sensitivity in 10 years for $\sin^2 2\theta_{13} (true) = 0.1$

Hierarchy sensitivity more for higher octant and higher θ_{13}

$$P_{e\mu} \sim \sin^2 \theta_{23} \sin^2 2\theta_{13}$$

Hierarchy sensitivity : Hyper-Kamiokande

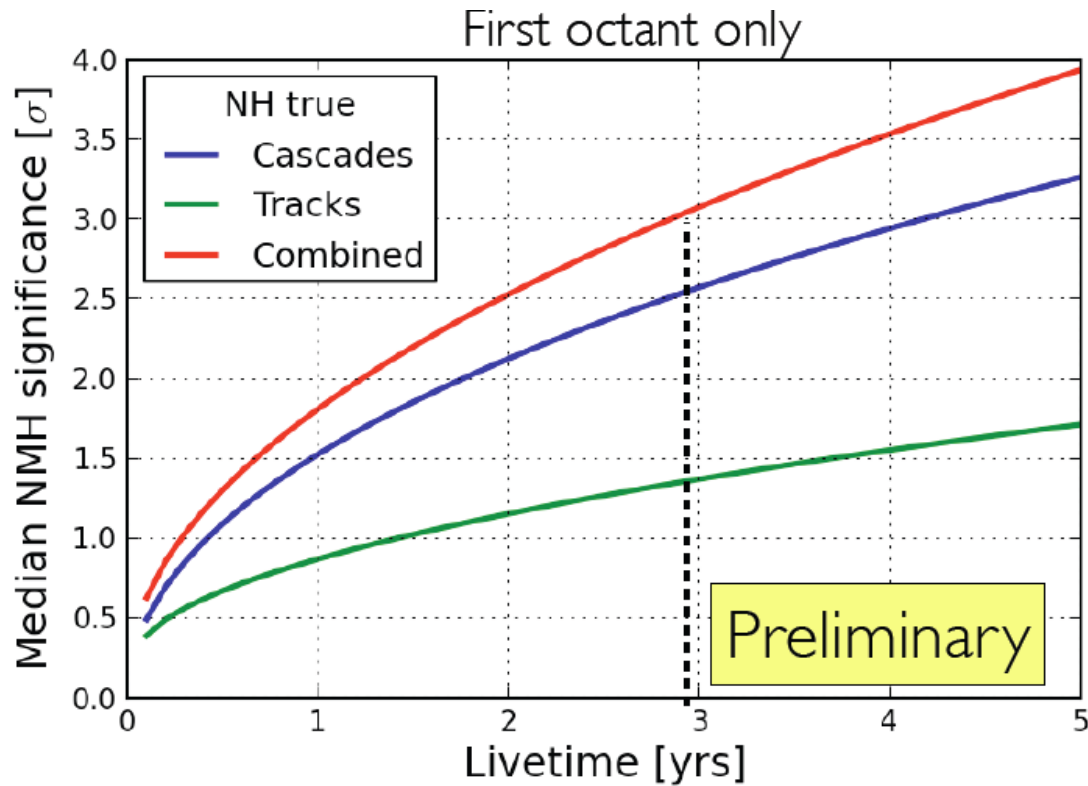
arXiv: 1109.3262 (HK Collaboration)



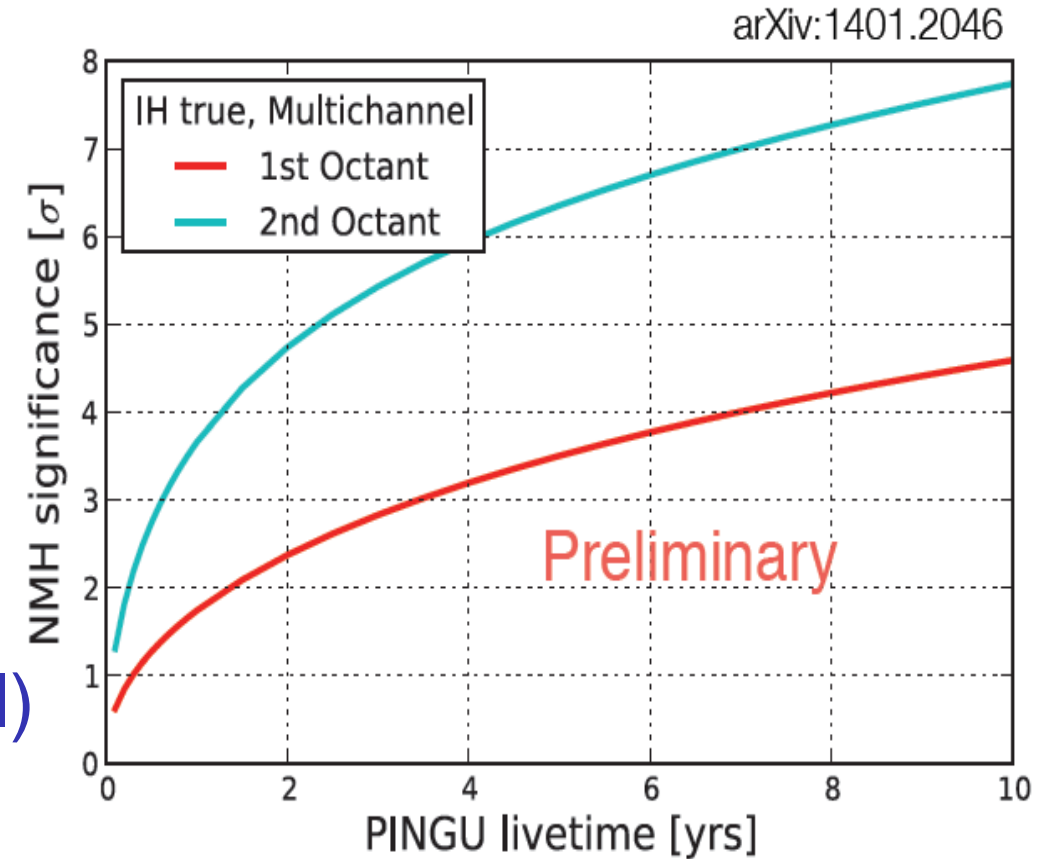
Sensitive to both electrons and muons

3σ sensitivity in approximately in 5 years for $\sin^2 2\theta_{13} = 0.08$

Hierarchy sensitivity : PINGU



Initial baseline geometry : 40 new strings and 60 optical modules in the deep core region of Icecube



➤ 3σ in ~ 3 yrs for 1st octant (multichannel)

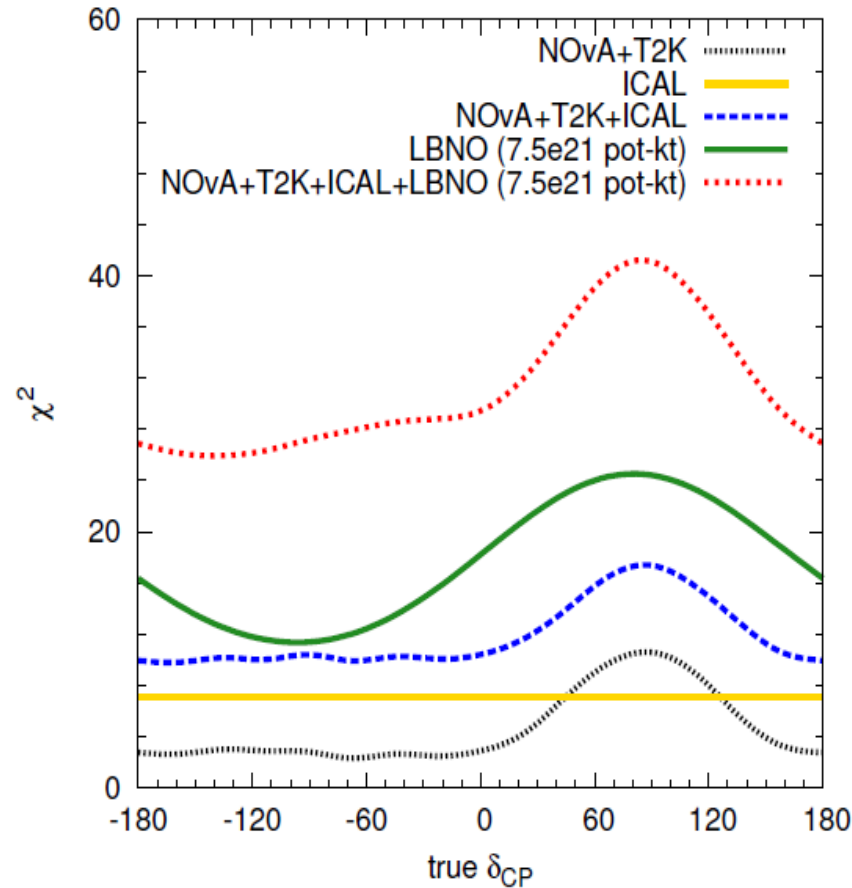
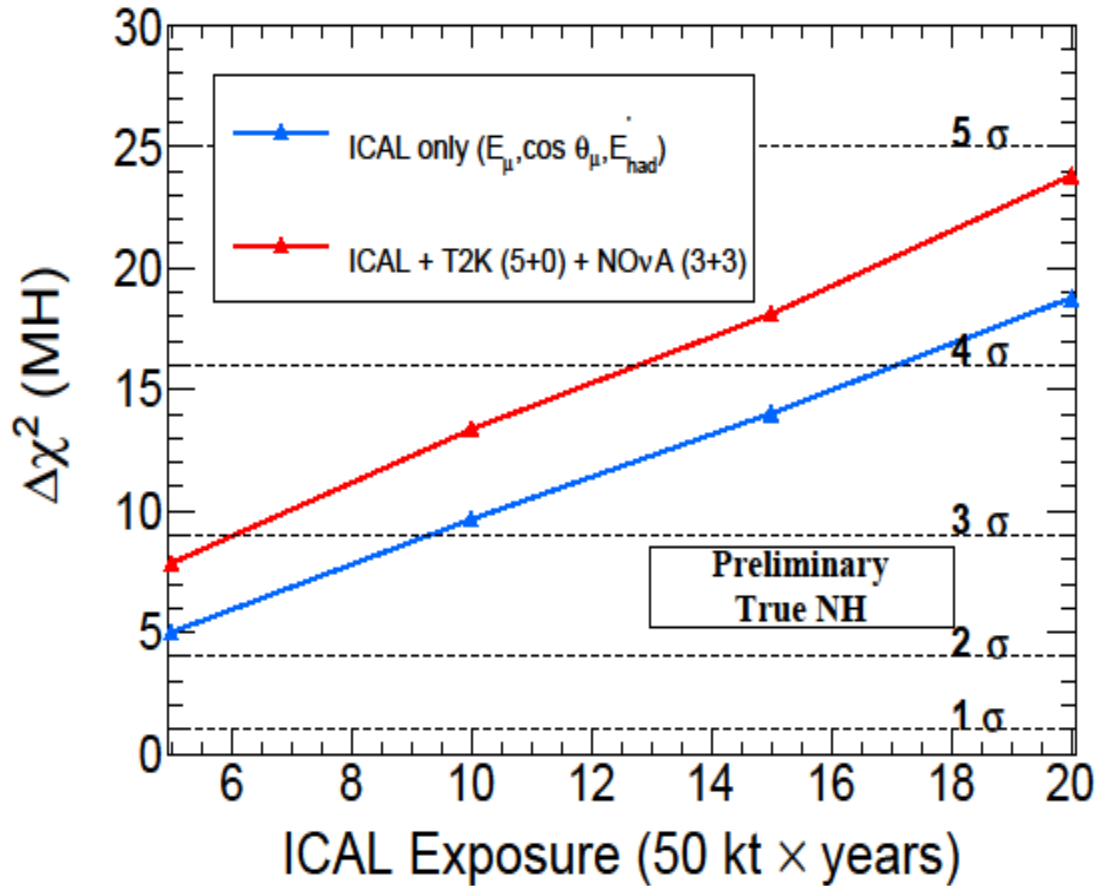
Including Cascades important

Talk by K. Clark , ICHEP 2014



Hierarchy Sensitivity: Atmospheric + LBL

$$\sin^2 2\theta_{13} = 0.1, \sin^2 2\theta_{23} = 0.5$$



Sensitivity improves by adding INO-ICAL



Reduced exposure for LBNO including Available information



3σ median sensitivity in 6 years with 50 kton ICAL by adding T2K and NoVA

Economizing configurations --- staged approach

Ghosh, Ghoshal, S.G., Raut, 2013. Ghosh, Thakur, Choubey, 2013, Blennow, Schwetz, 2012

Hierarchy Sensitivity : reactor neutrinos

$$P_R(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \left\{ \begin{aligned} &\cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21} \\ &+ \sin^2 2\theta_{13} \sin^2 \theta_{12} \left(\cos 2\Delta_{31} \sin^2 \Delta_{21} - \frac{1}{2} \sin 2\Delta_{31} \sin 2\Delta_{21} \right) \end{aligned} \right\}$$

Maxima for $\sin^2 \Delta_{21}$ (SPMIN)

Precise value of θ_{12}

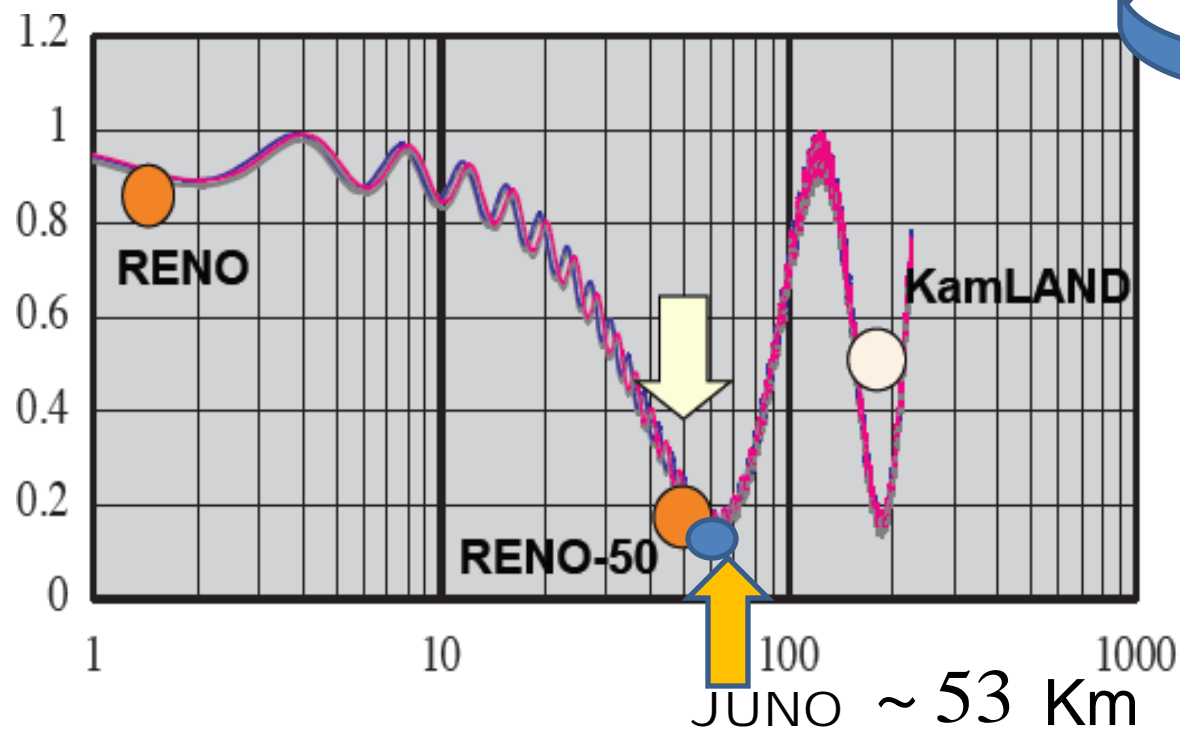
Bandyopadhyay, Choubey, S.G. 2003

Bandyopadhyaya, choubey, S.G, Petcov, 2005

Minakata

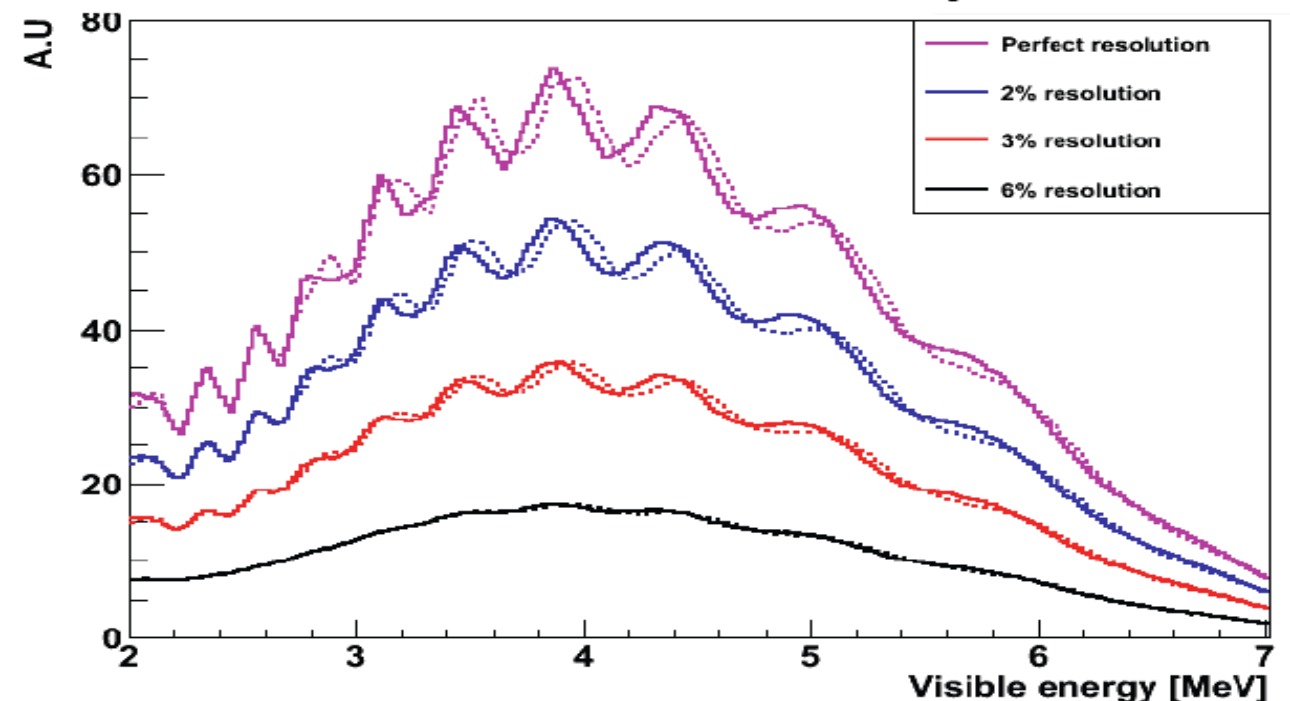
Petcov, Piai, 2001,

Choubey, Petcov, Piai, 2003



Hierarchy sensitivity

Distortions in the energy spectrum

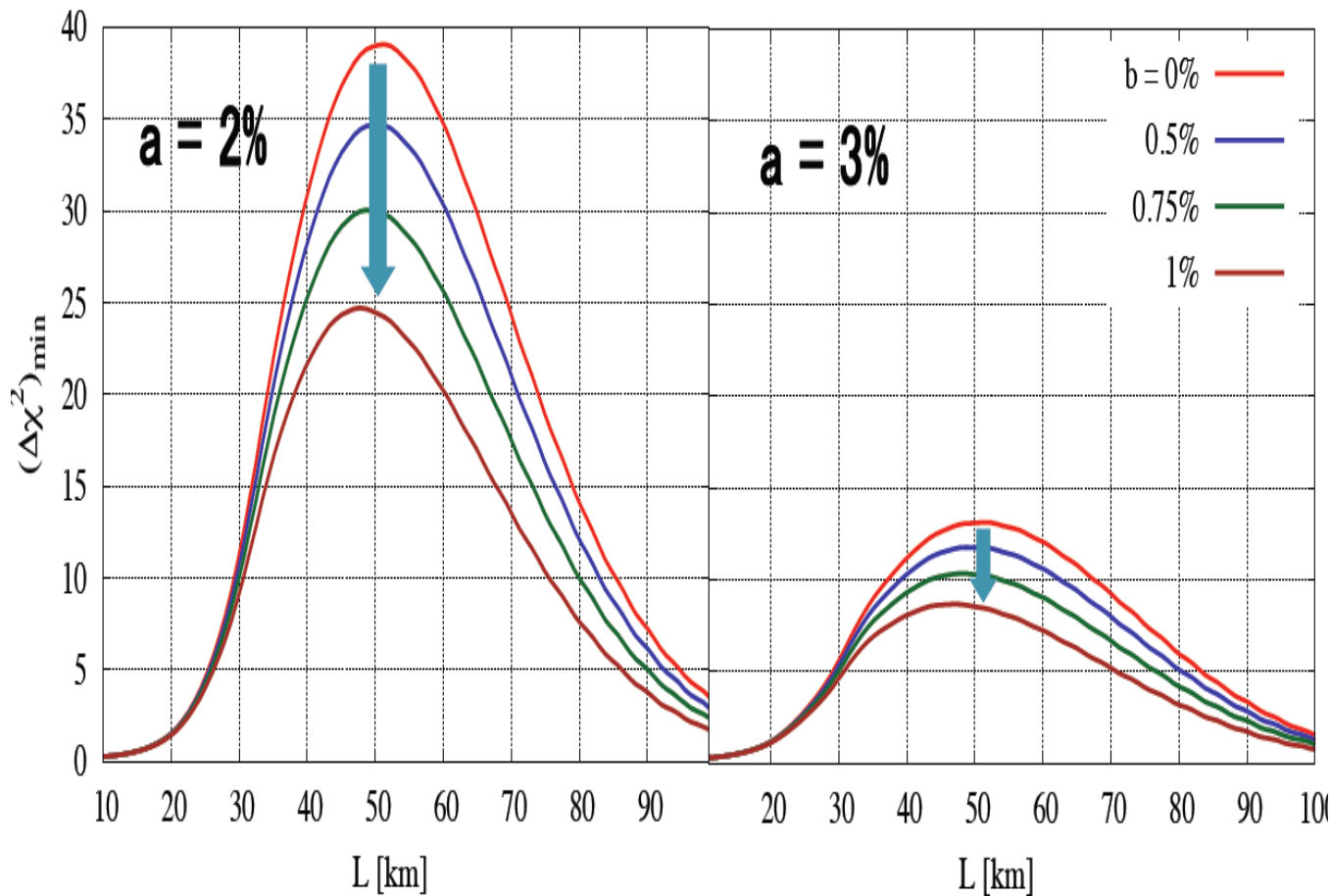


Better than 3% energy resolution needed

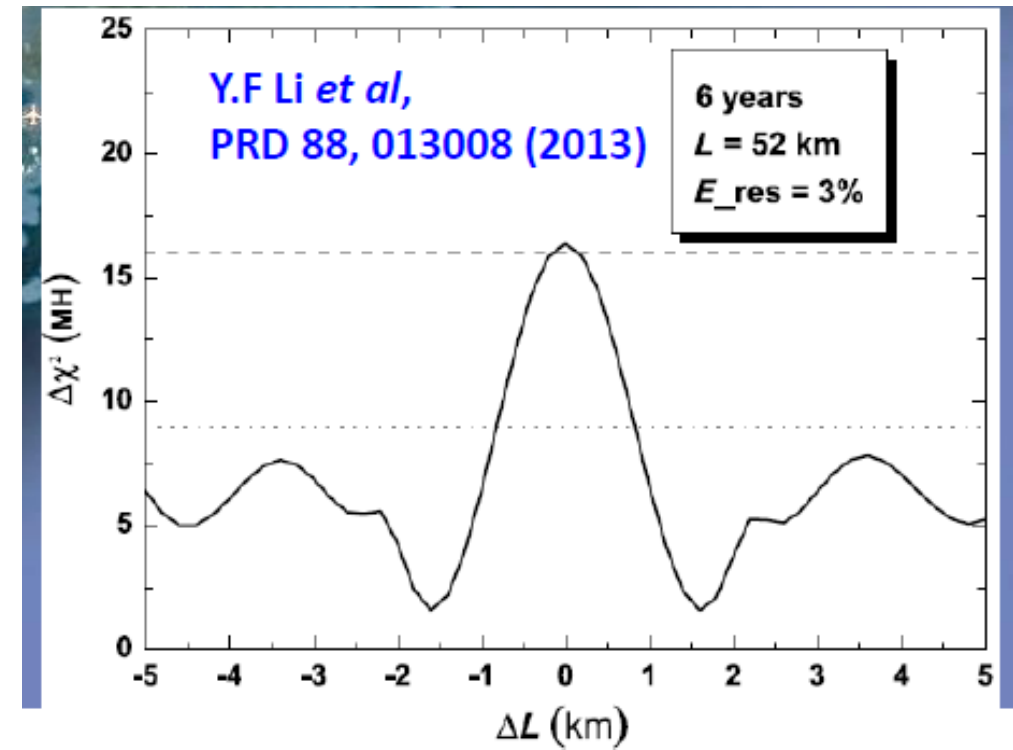
Figs : S.Seo RENO-50 workshop (2013)

Sensitivity to mass hierarchy: reactor neutrinos

RENO -50



JUNO



$$\frac{\sigma_E}{E} = \frac{a}{\sqrt{E/\text{MeV}}} + b$$

Energy non-linearity correction important for shape analysis < 1% understanding of energy scale

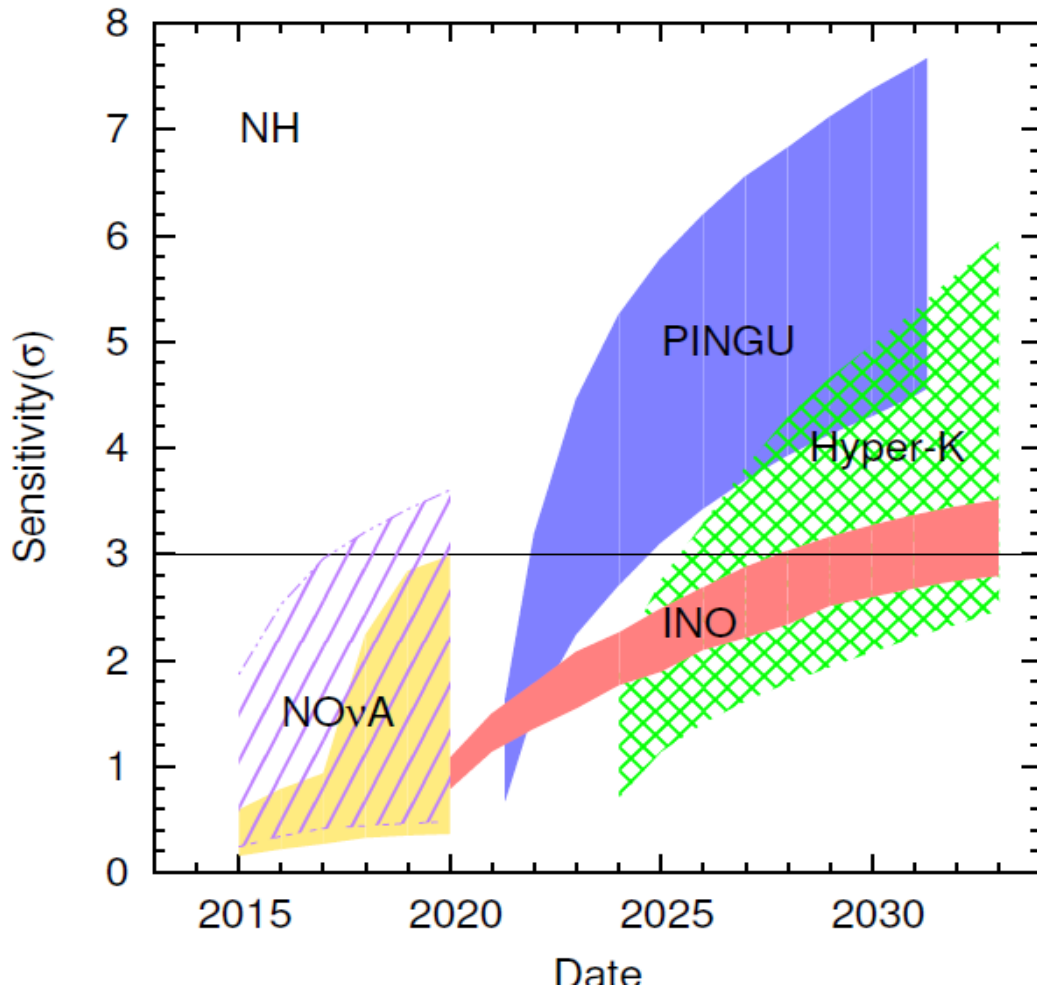
Y.Takaesu et al. JHEP05(2013)131

Talk by L. Zhan. ICHEP 2014

Hierarchy sensitivity in future experiments

Hierarchy sensitivity of NOvA atmospheric experiments

After Blenow et al. 1311.1822



NOvA δ_{CP}
 Atmospheric θ_{23}
 INO/SK $40^\circ - 50^\circ$
 Pingu : $38.7^\circ - 51.3^\circ$

NoVA : $3\nu + 3\bar{\nu}$
 INO : arXiv:1406.3689
 HK : arXiv 1109.3262
 PINGU: arXiv 1401.2046

The lower end of the bands denote worst sensitivity
 Pingu/HK huge statistics help for higher 2-3 angle

For favourable CP values early hint from Nova
 and for unfavourable CP values from NOvA + INO

Different statistical procedure followed by different groups

Octant Degeneracy

$$P_{\mu\mu} = 1 - \sin^2 2\theta_{23} \sin^2 \Delta + \text{sub leading terms}$$

$$P_{\mu\mu}(\theta_{23}) = P_{\mu\mu}(\pi/2 - \theta_{23})$$

Fogli and Lisi '96

Intrinsic octant degeneracy

$$P_{e\mu} \simeq \sin^2 \theta_{23} \sin^2 2\theta_{13} \frac{\sin^2(1-\hat{A})\Delta}{(1-\hat{A})^2} + \alpha \sin 2\theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos(\Delta - \delta_{CP}) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin(1-\hat{A})\Delta}{(1-\hat{A})}$$

$$P_{\mu e}(\theta_{13}, \theta_{23}, \delta_{CP}) = P_{\mu e}(\theta'_{13}, \theta'_{23}, \delta'_{CP})$$

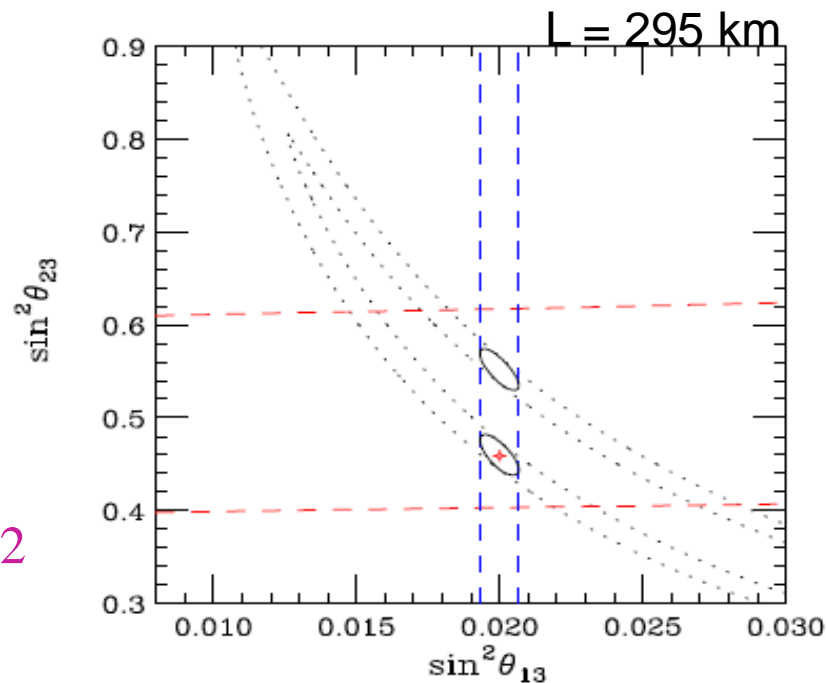
Generalized Octant Degeneracy

Agarwalla, Prakash, Sankar, 2013

Chatterjee, Ghosal, Goswami, Raut, 2013

Octant sensitivity
Correlated to θ_{13}
Accelerator +
Reactor data helpful

Huber, Lindner, Winter, 2002
Hiraide et al., 2006

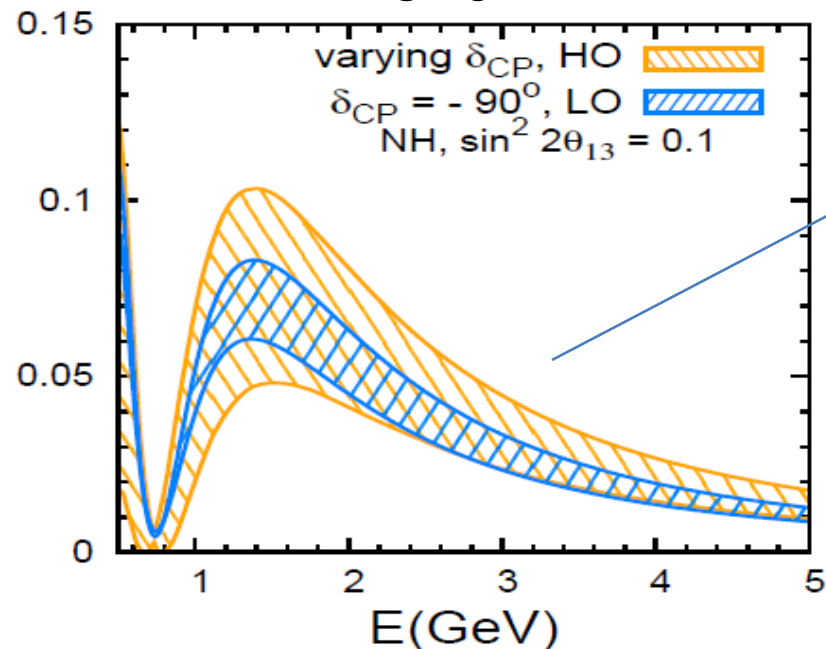


Coloma, Minakata, Parke, 2014

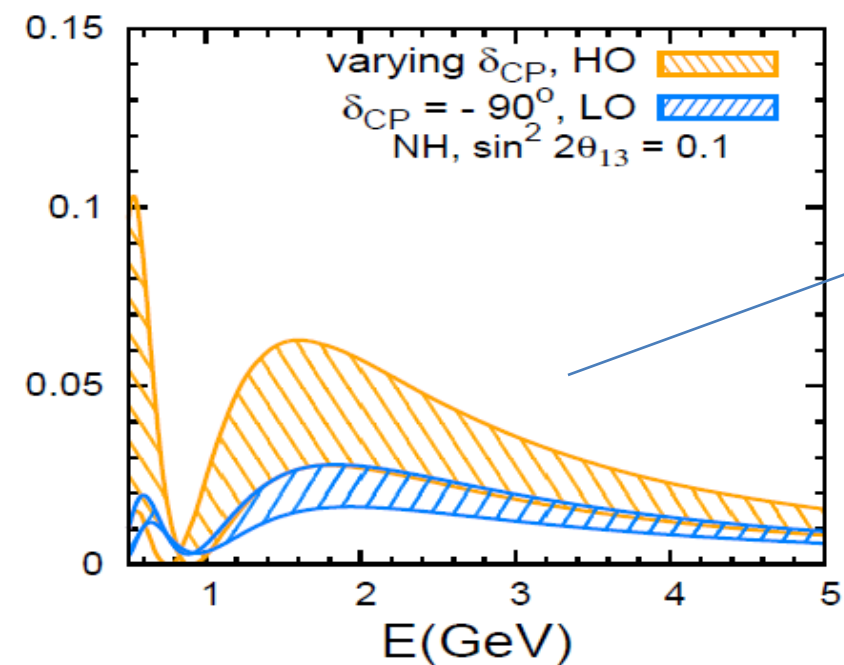
Depends on L/E
Spectrum information useful
Unknown δ_{CP} can be a problem

Octant degeneracy and δ_{CP}

$L = 810$ km

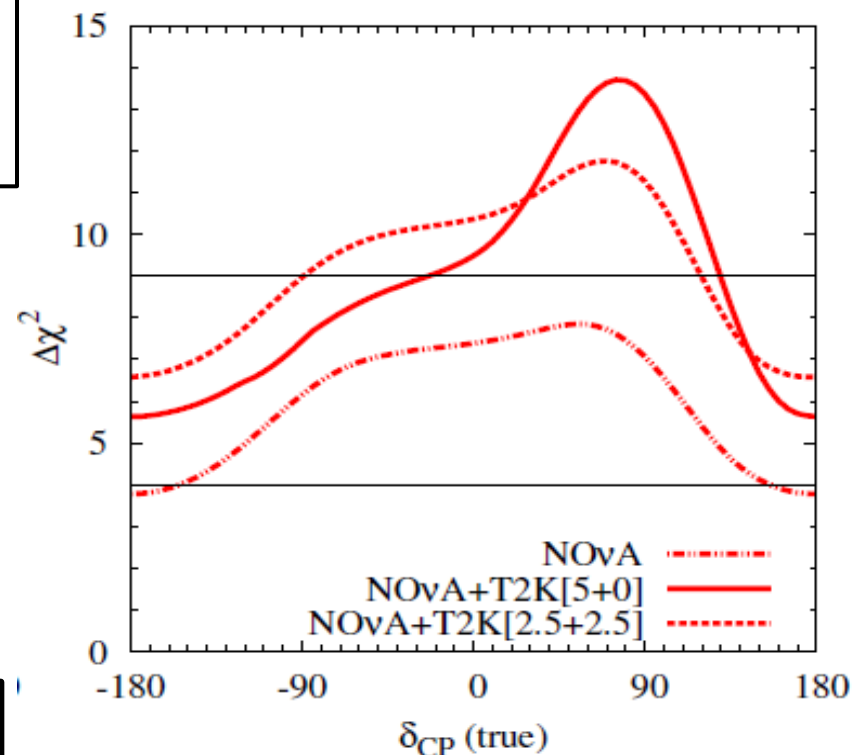


For $\nu: \delta_{CP} = -90^\circ$
and LO bad



For $\bar{\nu}: \delta_{CP} = -90^\circ$
and LO good

Octant Discovery, LO-IH true



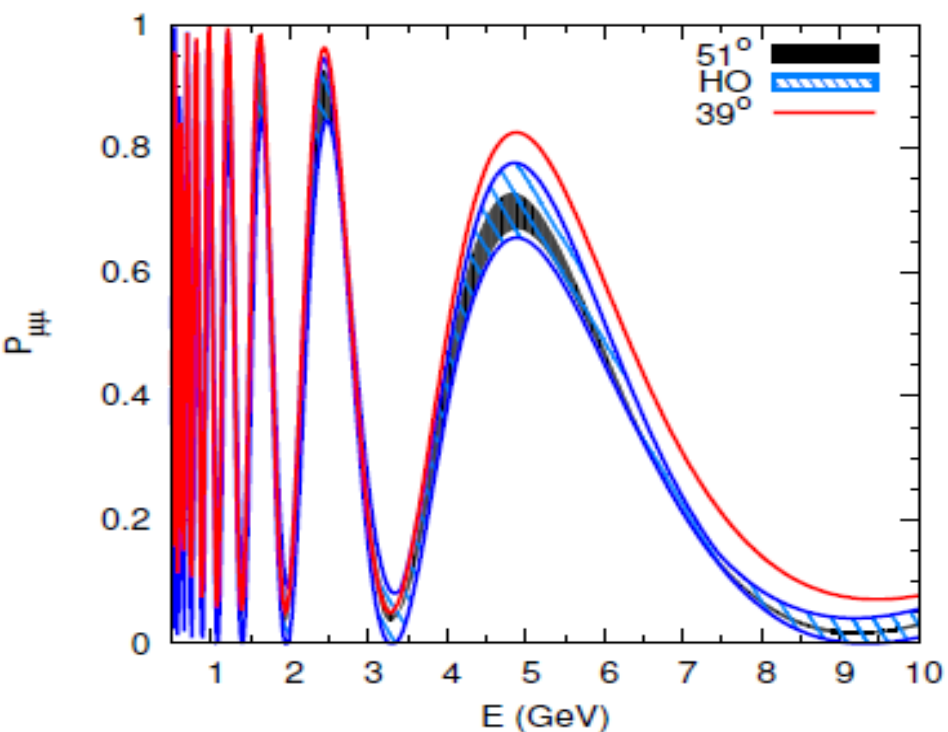
Agarwalla, Prakash, Umasankar 2013

Machado et al. 2013

Combination of ν and $\bar{\nu}$ can be helpful lifting octant degeneracy (depending on δ_{CP})

Talk by S. Umasankar , ICHEP 2014

Octant Sensitivity: Atmospheric Neutrinos



$$P_{\mu\mu}^m \longrightarrow \sin^4 \theta_{23} \sin^2 2\theta_{13}^m \sin^2 (1.27 \Delta_{31}^m L/E)$$

Octant Sensitivity

Choubey, Roy, 2005

Near resonance

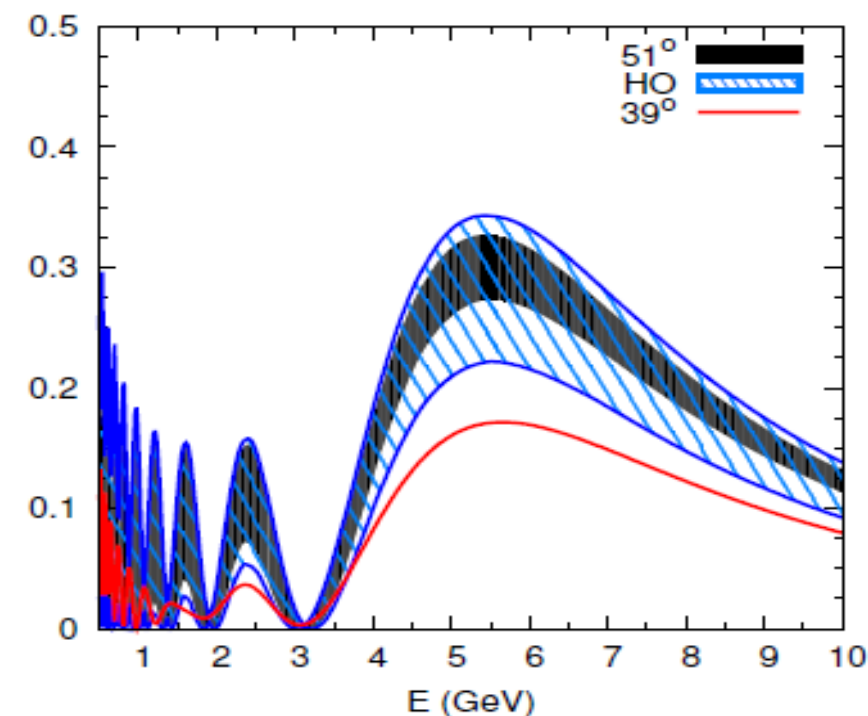
$$\sin^2 2\theta_{13}^m \approx 1$$

⇒ No $(\theta_{23} - \theta_{13})$ degeneracy

$$P_{\mu e}^m = \sin^2 \theta_{23} \sin^2 2\theta_{13}^m \sin^2 \left[1.27 (\Delta m_{31}^2)^m \frac{L}{E} \right]$$

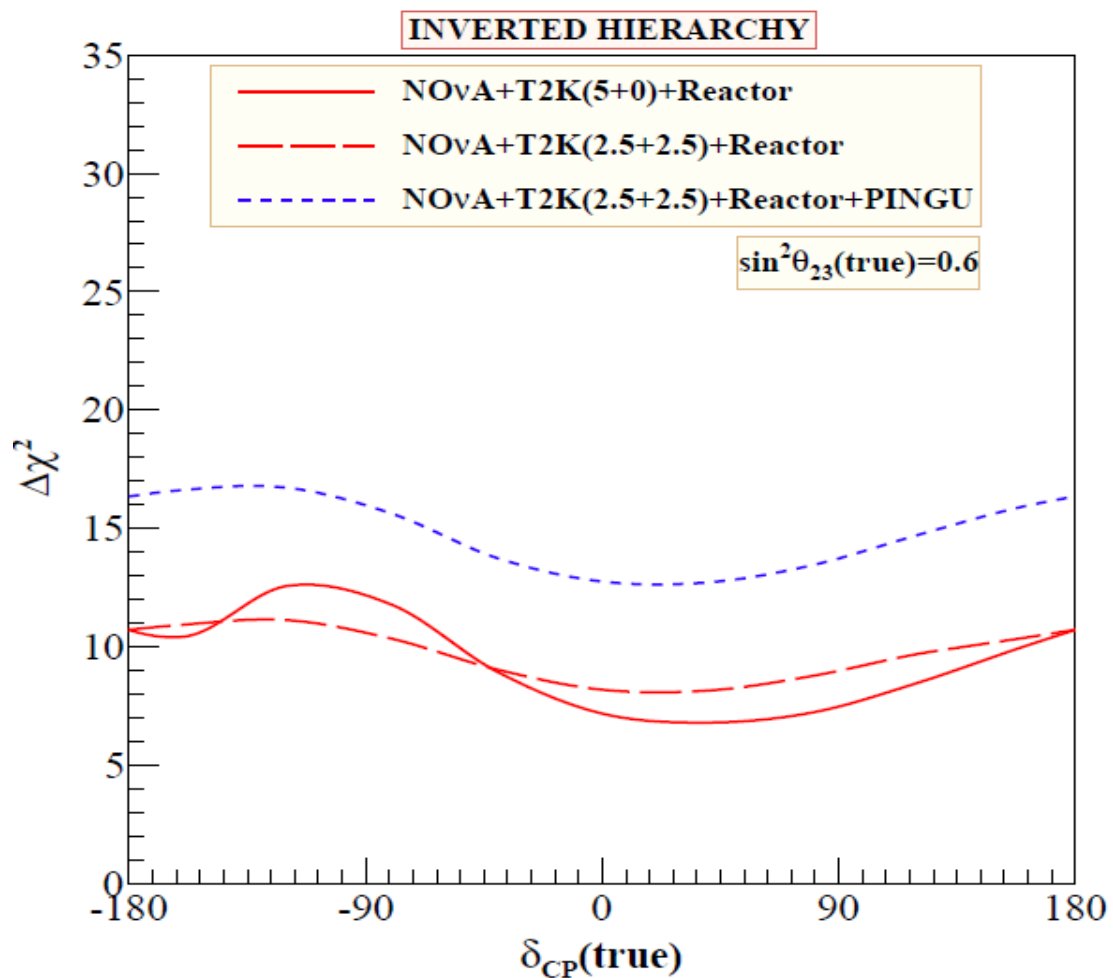
δ_{CP} effects subdominant

θ_{23} dependence of survival and conversion probabilities opposite



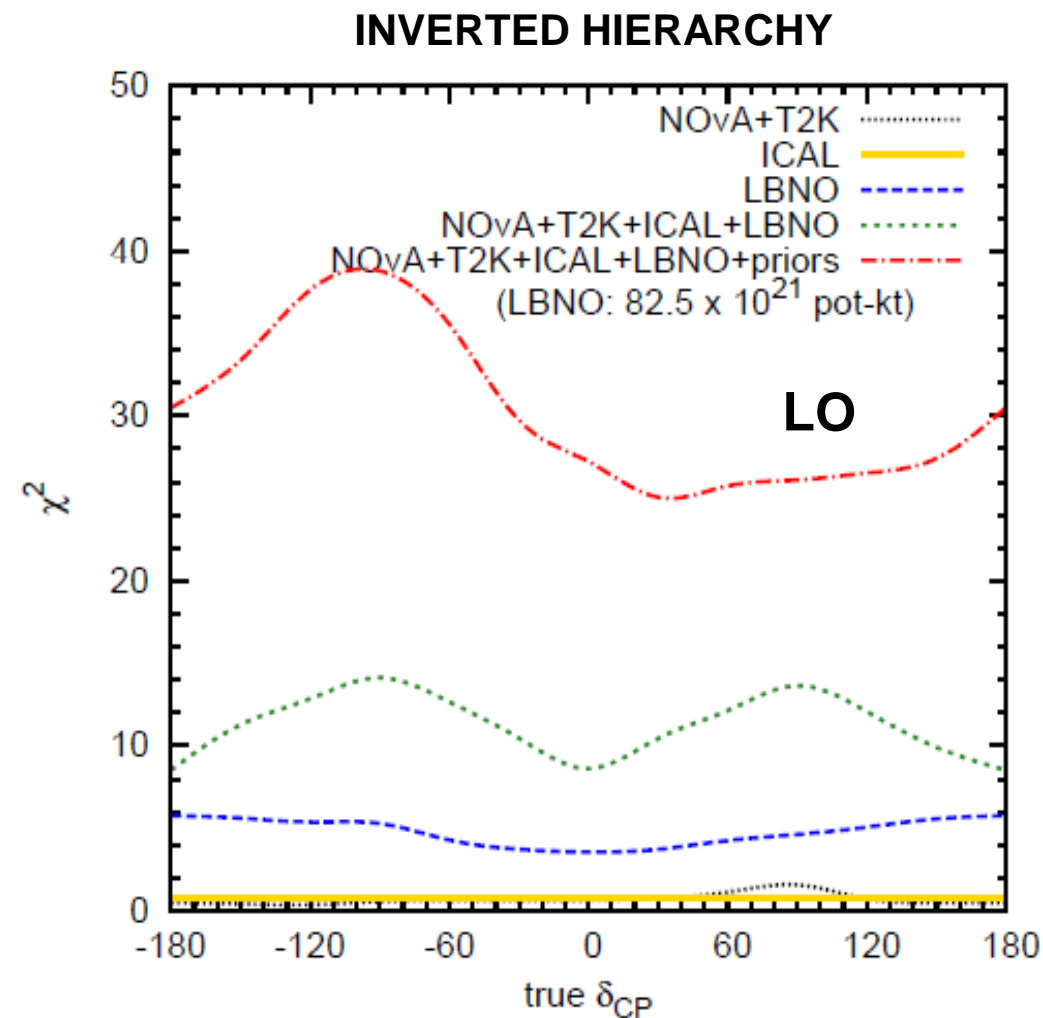
Chatterjee, Ghoshal, Goswami, Raut, 2013

Octant Sensitivity : atmospheric + LBL



Synergy between atmospheric and LBL experiments increase octant sensitivity

Choubey and Ghosh, 2013



Precision of 1-3 mixing angle plays a very important role

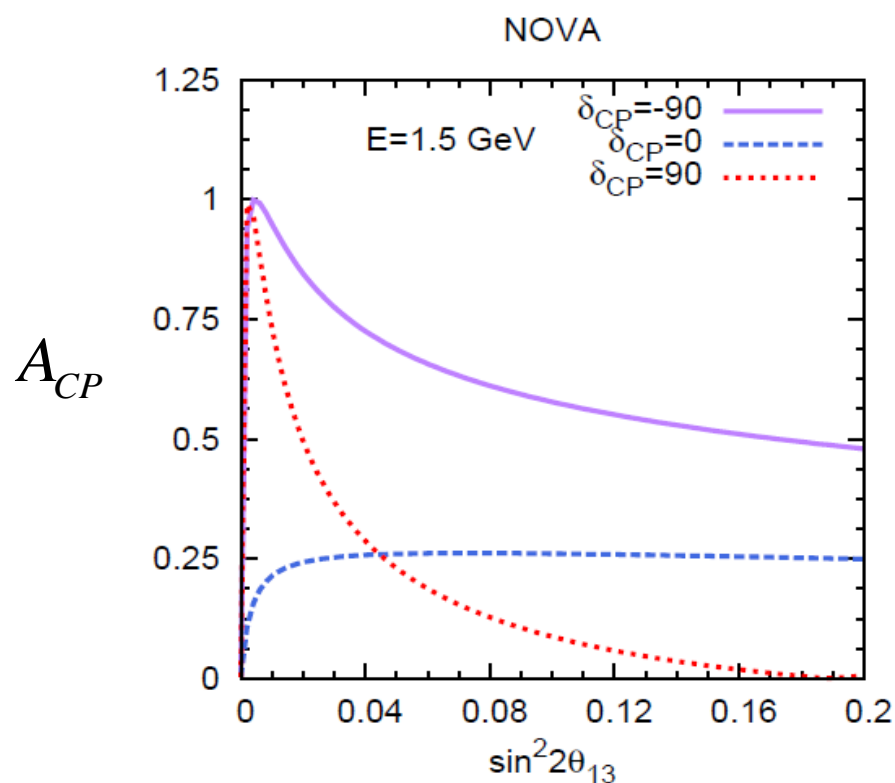
Ghosh, Ghosal, Goswami, Raut, 2013

CP violation in neutrino oscillations

- CP violation due to the phase δ_{CP}

$$P_{\mu e} - P_{\bar{\mu} e} = 4s_{12}c_{12}s_{13}c_{13}^2s_{23}c_{23} \sin \delta_{CP} \left[\sin \frac{\Delta m_{21}^2 L}{2E} + \sin \frac{\Delta m_{23}^2 L}{2E} + \sin \frac{\Delta m_{31}^2 L}{2E} \right]$$

Genuine three flavour effect : require all angles and Δm_{21}^2 to be non-zero

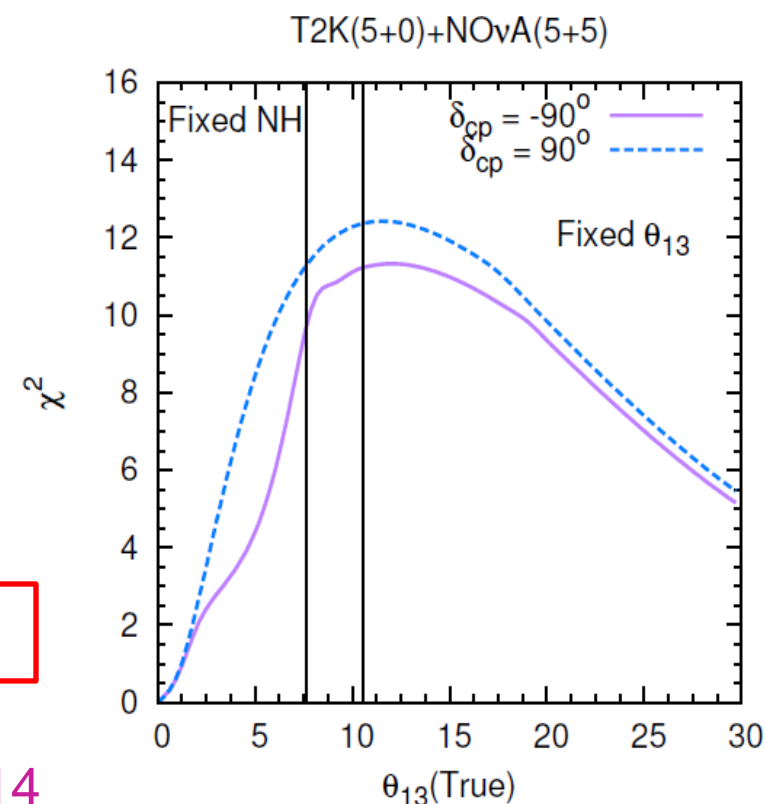


$$A_{CP} = \frac{P_{\mu e} - P_{\bar{\mu} e}}{P_{\mu e} + P_{\bar{\mu} e}} \sim \frac{\sin \delta_{CP}}{\sin \theta_{13}}$$

$$\chi^2 \sim \frac{P(\delta_{CP}) \sin^2 2\theta_{13}}{Q \sin^2 \theta_{13} + R(\delta_{CP}) \sin 2\theta_{13}}$$

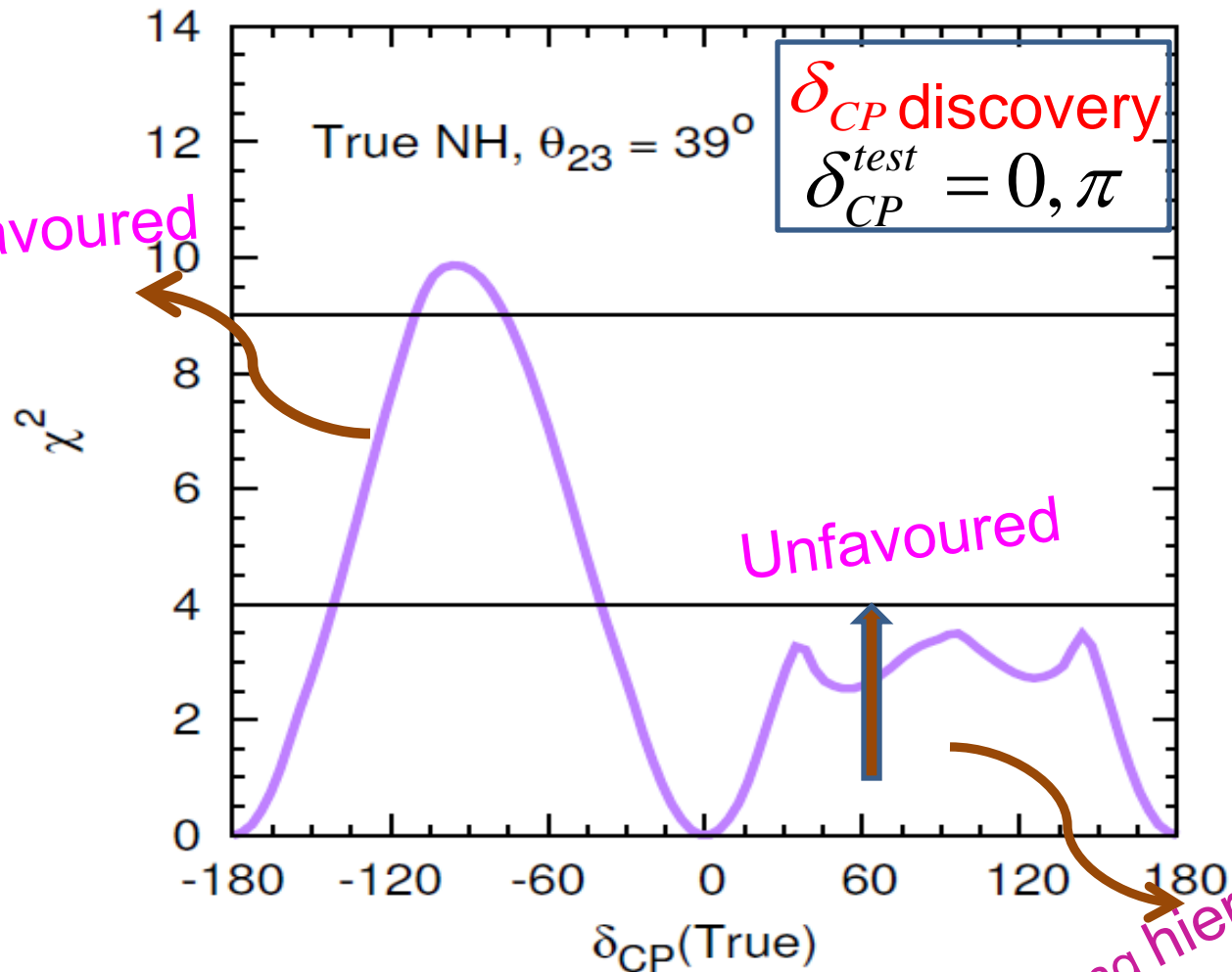
Current θ_{13} range optimal

Ghosh, Ghoshal, Goswami, Raut 2014



δ_{CP} in long-baseline experiments

NOVA(3+3)+T2K(5+0)



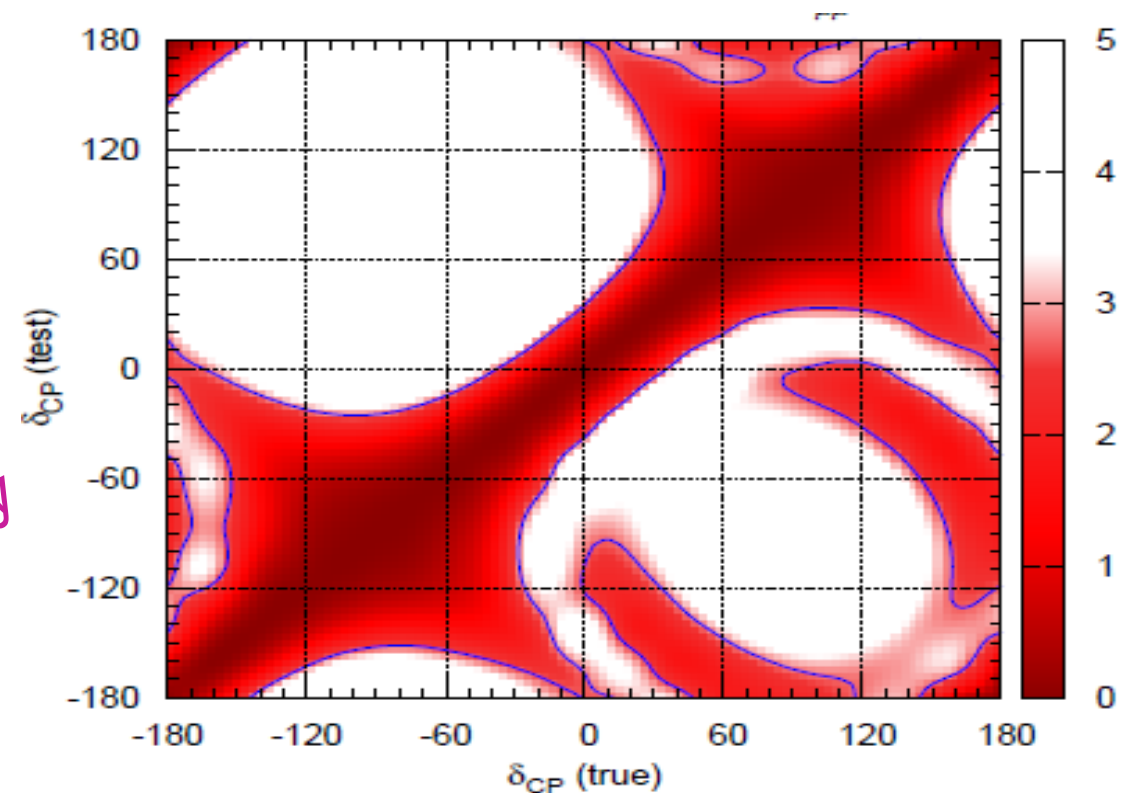
2σ for 24% values of δ_{CP}

Talk by L. Escudero, ICHEP 2015

$$\chi^2 = \min \frac{(N_{ex}(\delta_{CP}^{tr}) - N_{th}(\delta_{CP}^{test}))^2}{N_{ex}(\delta_{CP}^{tr})}$$

$$\chi^2 = \chi_\nu^2 + \chi_{\bar{\nu}}^2$$

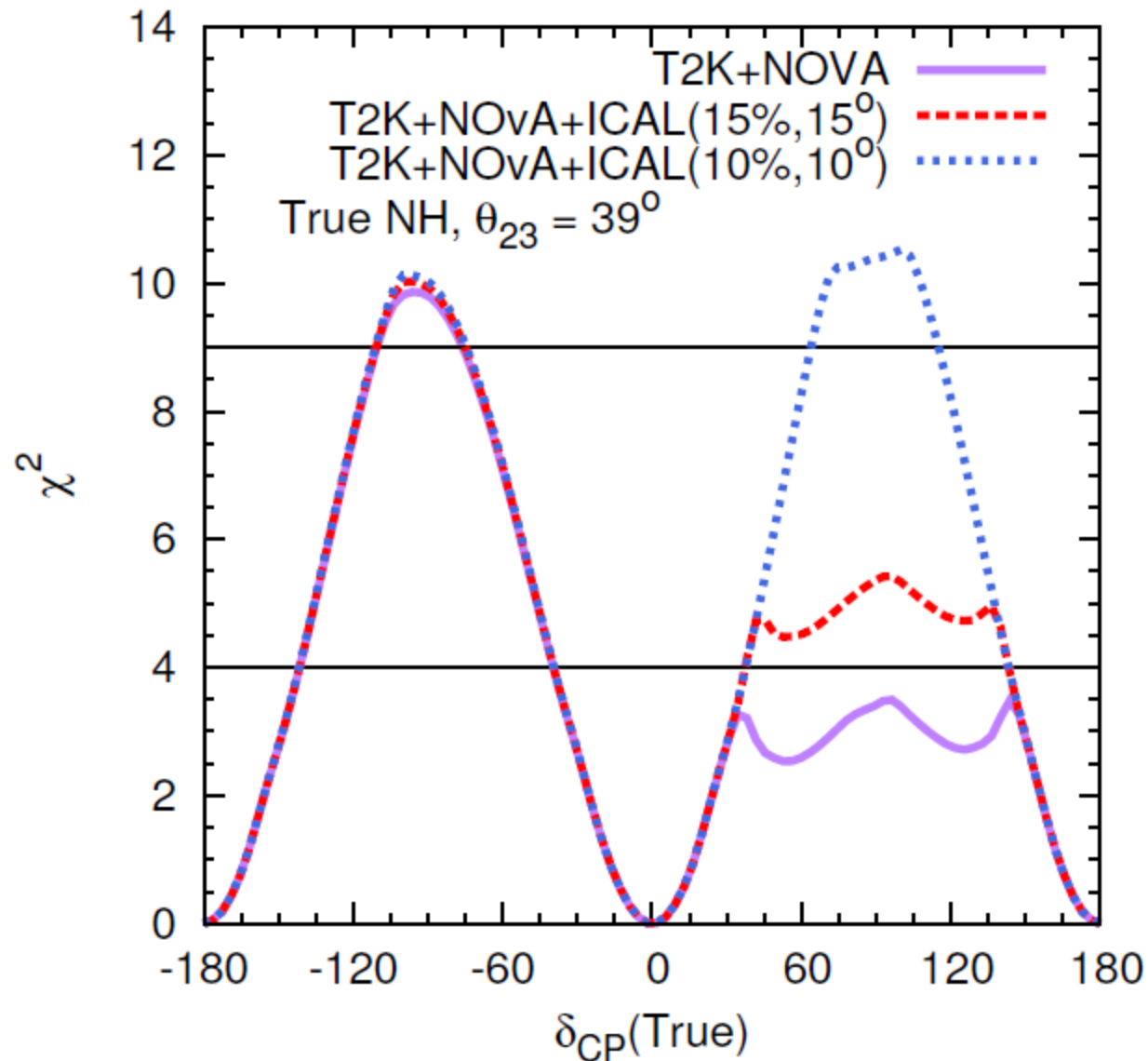
δ_{CP} precision : δ_{CP} varied over full range



Ghosh, Ghoshal, Goswami, Raut (2014)

CP sensitivity : atmospheric + LBL

T2K (5+0) , NOvA (3+3) + ICAL (500 kt yr)



Adding hierarchy information from INO-ICAL data increases the CP sensitivity in wrong hierarchy region

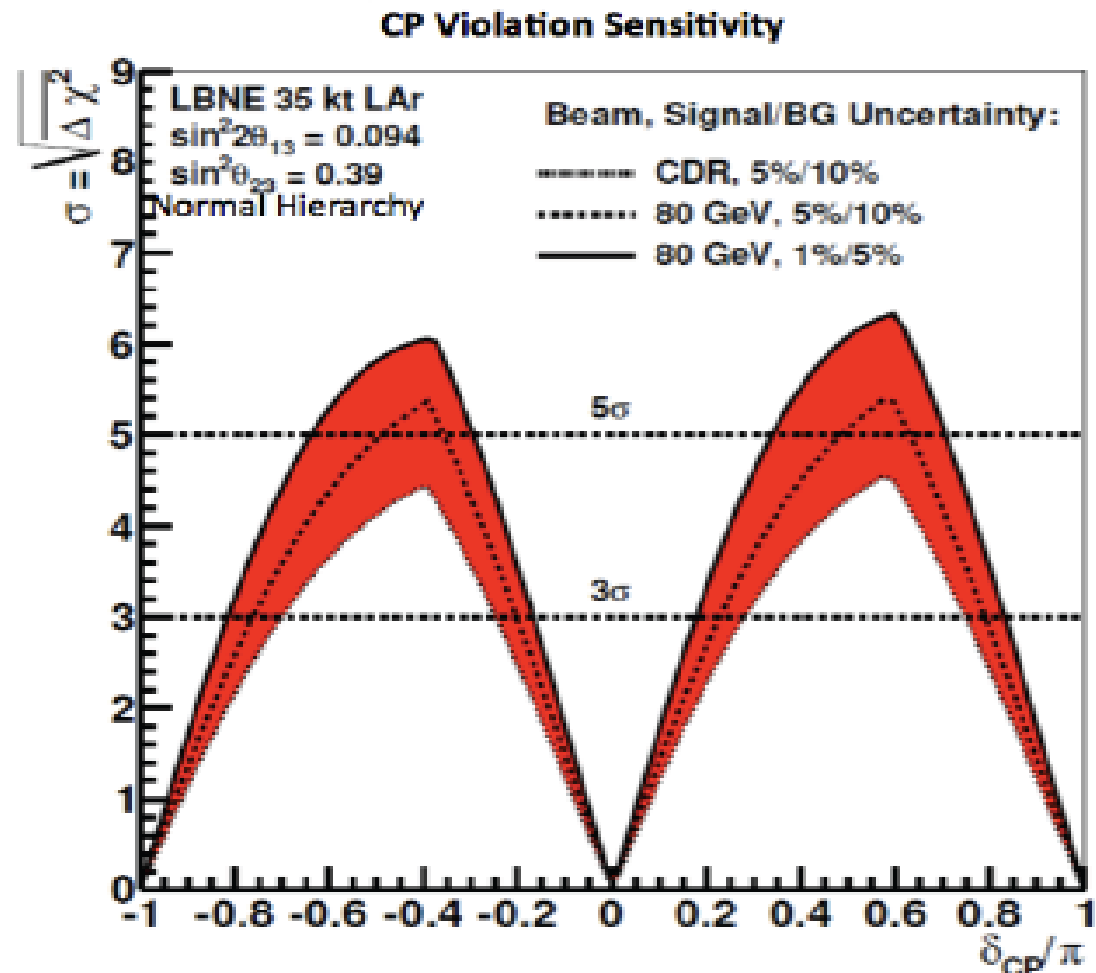
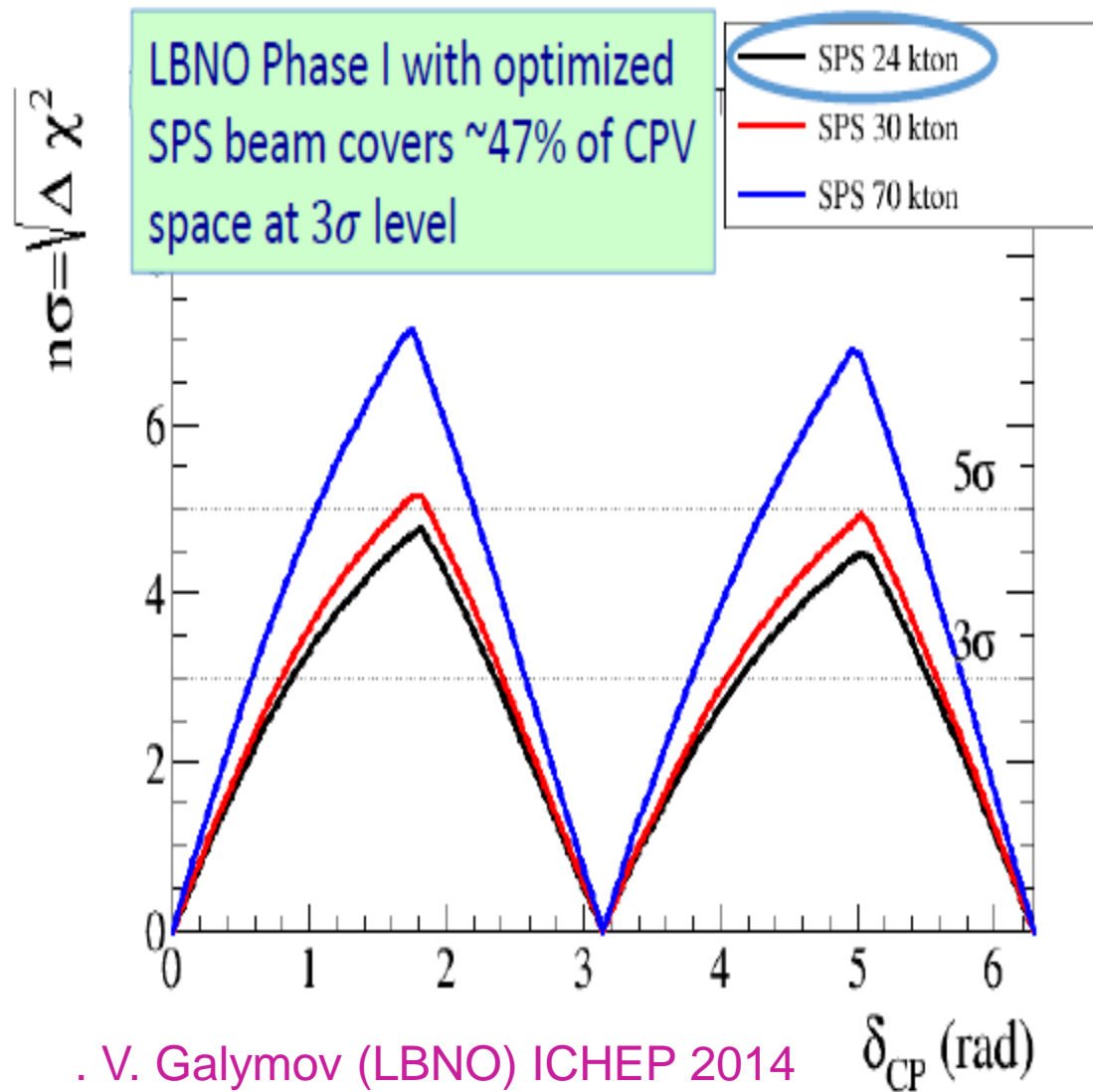
50% increase in CP coverage

For unfavorable CP values first hint of non-zero δ_{CP} may come after adding ICAL data

(also true for other atmospheric experiments)

Ghosh, Ghosal, Goswami, Raut (2013),

δ_{CP} in Long-Baseline experiments



Z. Djurcic (LBNE), ICHEP 2014

V. Galymov (LBNO) ICHEP 2014

More than 5σ for some fraction of CP phases

See also talks by M. Dracos (ESS), M. Shaevitz (DAE δ DALUS), H. Tanaka (HK)

Status of sterile neutrinos oscillations

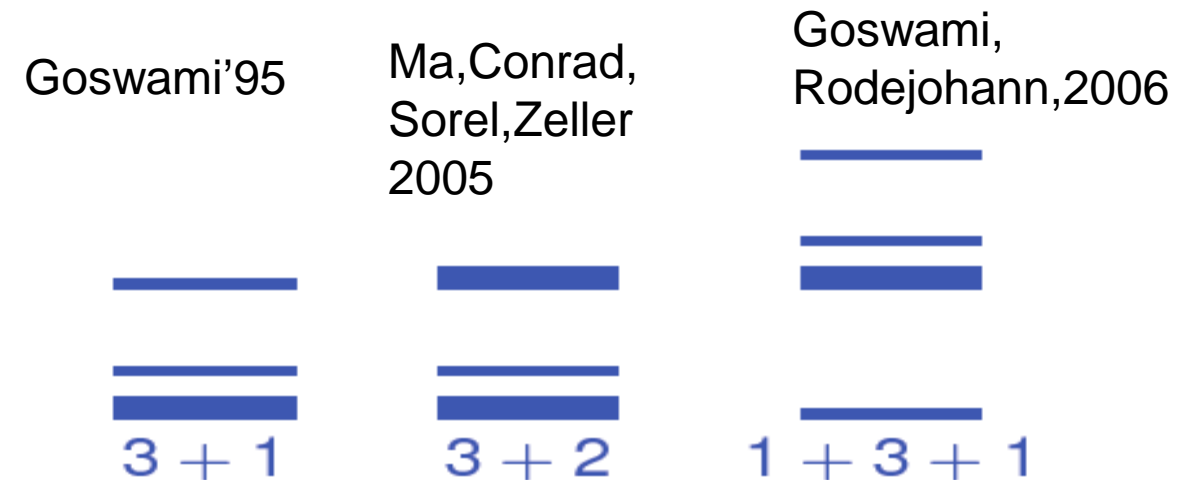
Evidences

- $\bar{\nu}_\mu - \bar{\nu}_e$ oscillations reported in LSND and MiniBOONE
- Reactor Anomaly : Recalculated reactor fluxes are 3.5% more than the previous calculation
- Ga Anomaly : Deficit of ν_e from ^{51}Cr and ^{37}Ar sources in the reaction $^{71}\text{Ga} + \nu_e \rightarrow ^{71}\text{Ge} + e^-$

Future Projects :

Talks by L.Stanco, M. Shaevitz , B. David, W. Ketchum, J. Lagrange, ICHEP 2014

Status of sterile neutrino fits



J. Kopp, Neutrino 2014

Appearance data can be fit in all three schemes 3+2 and 1+3+1 better

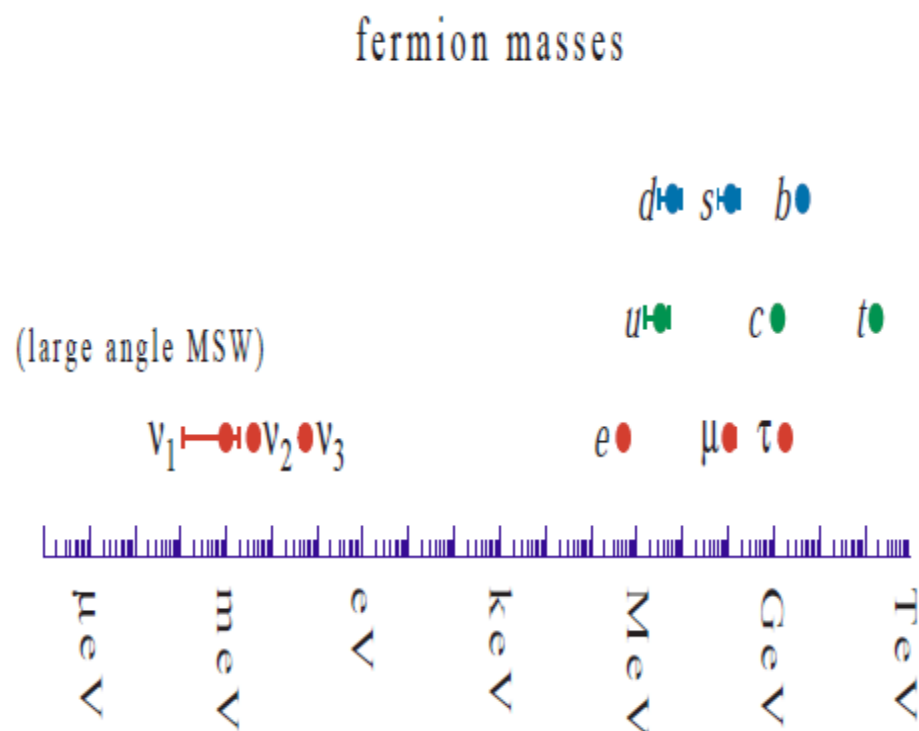
Severe tension when disappearance data is added

Kopp, Machado, Maltoni, Schwetz, Giunti-et al.
Conrad et al.

Two fundamental questions

- Why neutrino masses are so small ?

- Why neutrino mixing angles so different ?



Quark Mixing angles

Neutrino mixing angles

$$\theta_{12} = 13^\circ$$

$$\theta_{23} = 2.3^\circ$$

$$\theta_{13} = 0.2^\circ$$

$$\delta_{CP} = 68.5^\circ$$

$$\theta_{12} = 33.5^\circ$$

$$\theta_{23} = 49^\circ$$

$$\theta_{13} = 8.5^\circ$$

$$\delta_{CP} = 250^\circ$$

Seesaw, Radiative mass generation,
Seesaw + radiative

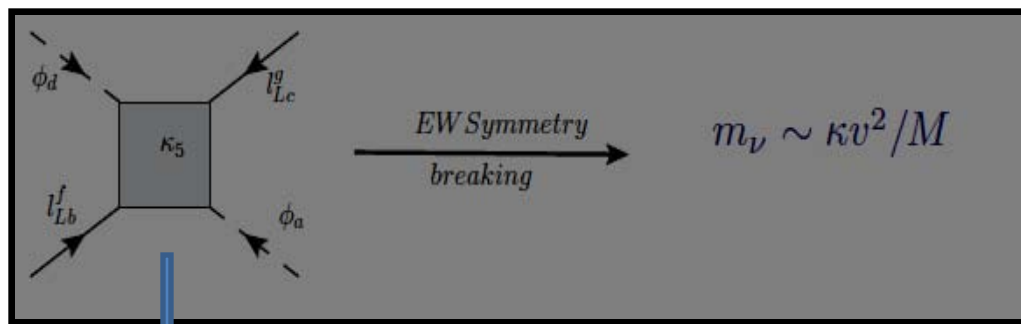
Flavour symmetries, Anarchy
TBM, QLC ...

Seesaw and its implications : Neutrino connections

Standard Model is an effective theory and one can add non-renormalizable operators

$$\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_{eff}^{d=5} + \mathcal{L}_{eff}^{d=6} + \dots, \quad \text{with} \quad \mathcal{L}_{eff}^d \propto \frac{1}{\Lambda_{NP}^{d-4}} \mathcal{O}^d.$$

Dimension 5 : only one operator $\mathcal{L} = c_5 LLHH$ $c_5 = \kappa/M$ Weinberg, 1979



m_ν can be small for high $M \rightarrow 10^{15} \text{ GeV}$

Neutrinoless double beta decay

M. Malinsky, ICHEP 2014

GUTS

Lepton number violation

Majorana nature

SO(10)

SU(5)

Three ways to generate the above operator -- Type-I, Type-II, Type-III

Like sign di-lepton at LHC

Large light-heavy mixing

TeV scale seesaw

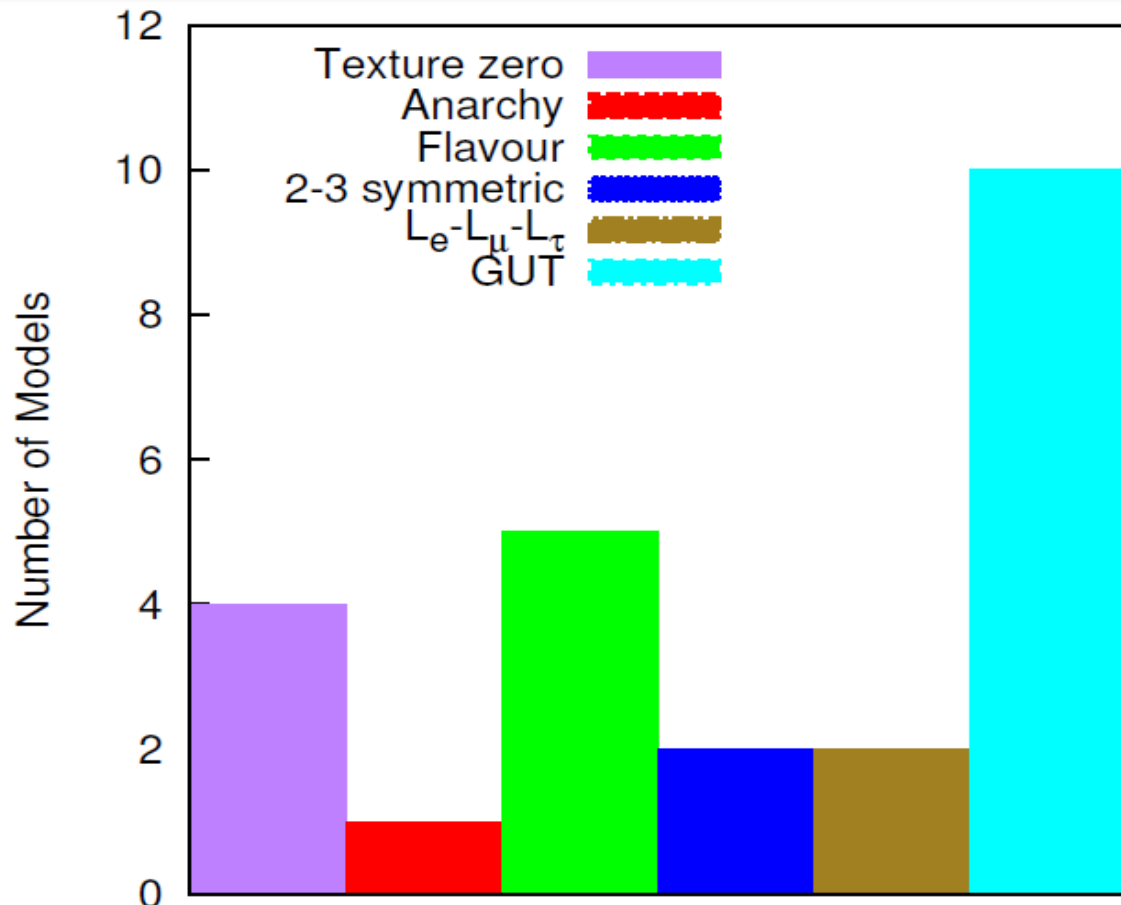
Can't be probed at LHC

Lepton Flavour Violation

Inverse Seesaw, Higher dim operators, textures

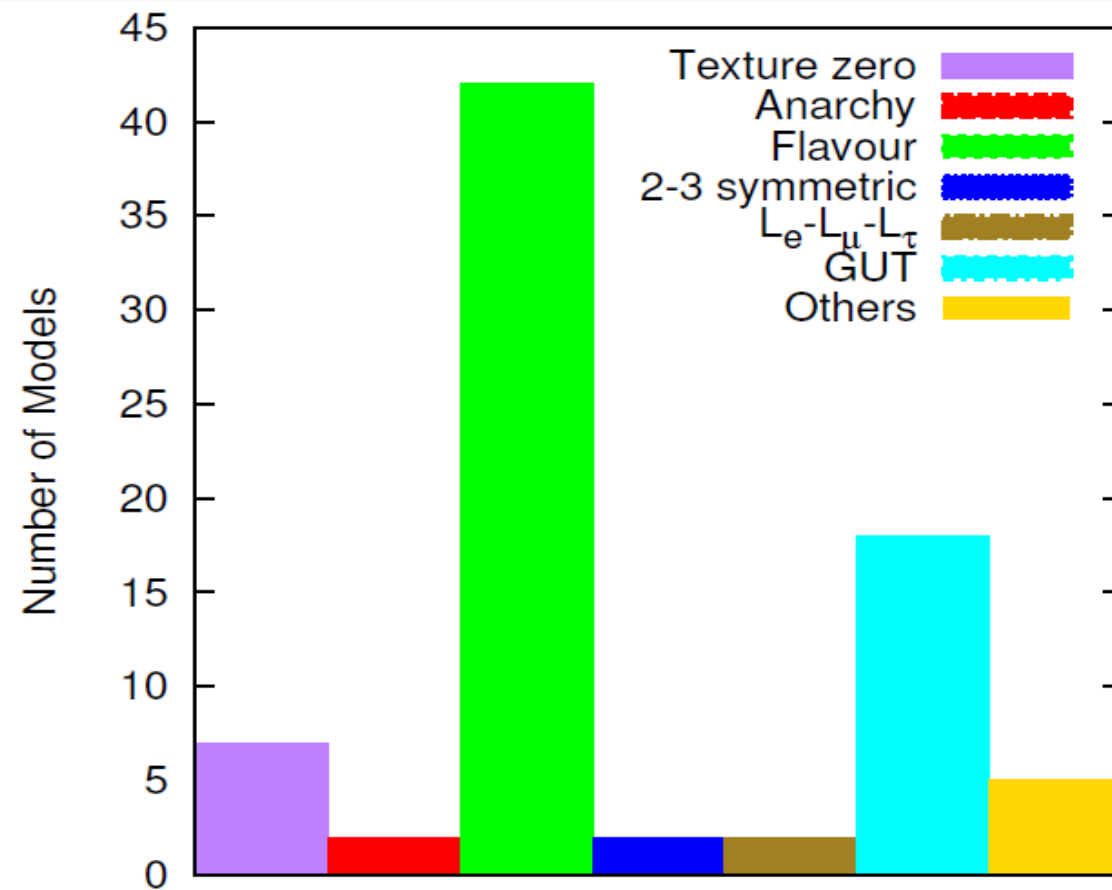
Talk by A. Blondel on search for heavy Neutrinos at Z and H factory, ICHEP 2014

Is there a case for precision measurements ?



Models from 0905.0146 (Albright)
that survive the present 3σ range

24 Models survive out of 86



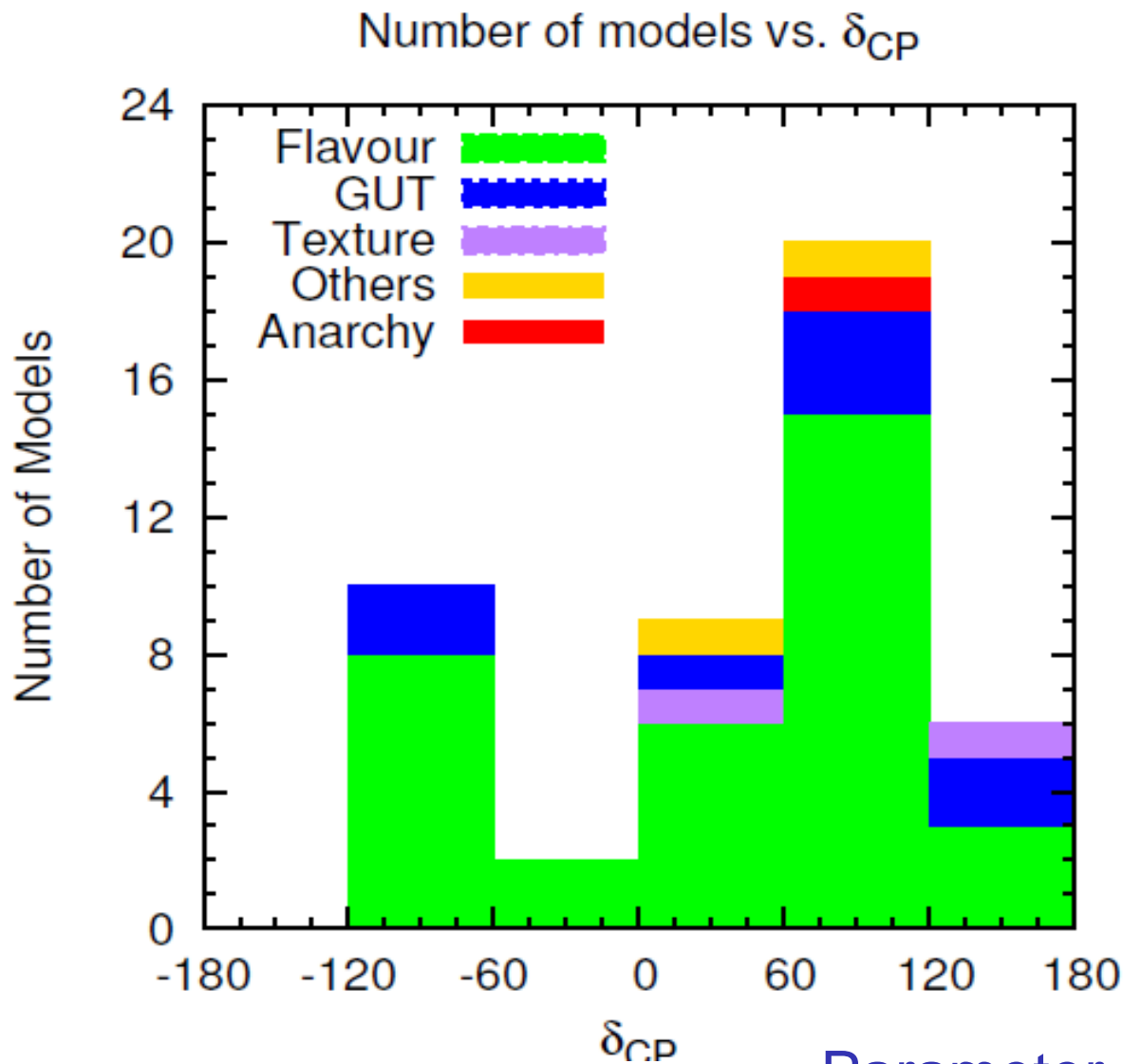
54 new models ! (incomplete survey)

Flavour boom

Difficult to beat theoreticians

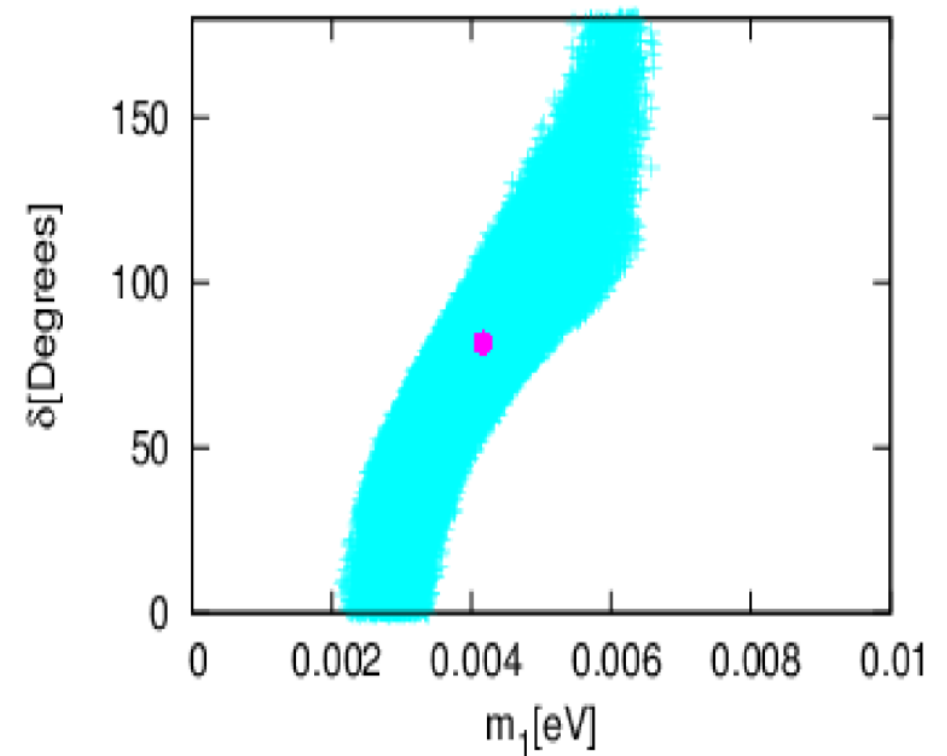
Bambhanya, Ghosh (2014)

Prediction for δ_{CP}



$$A_1 : \begin{pmatrix} 0 & 0 & X \\ 0 & X & X \\ X & X & X \end{pmatrix}$$

Frampton, Glashow, Marfatia. 2002
Xing 2002



Parameter correlation important

Bambhanya, Ghosh (2014)

Babu, Devi, Goswami, 2014
Liao, Marfatia, Whisnant, 2014

Concluding Remarks

- Impressive progress in determination of neutrino oscillation parameters
- Discovery of θ_{13} has opened the avenues for determination of mass hierarchy, octant of θ_{23} and δ_{CP}
- Many future experiments
- The findings of the current generation experiments will be crucial input
- Synergistic aspects between various experiments important
- Precision measurements help in disfavouring models but also many new models
- Parameter correlation may be important ...

Finally...

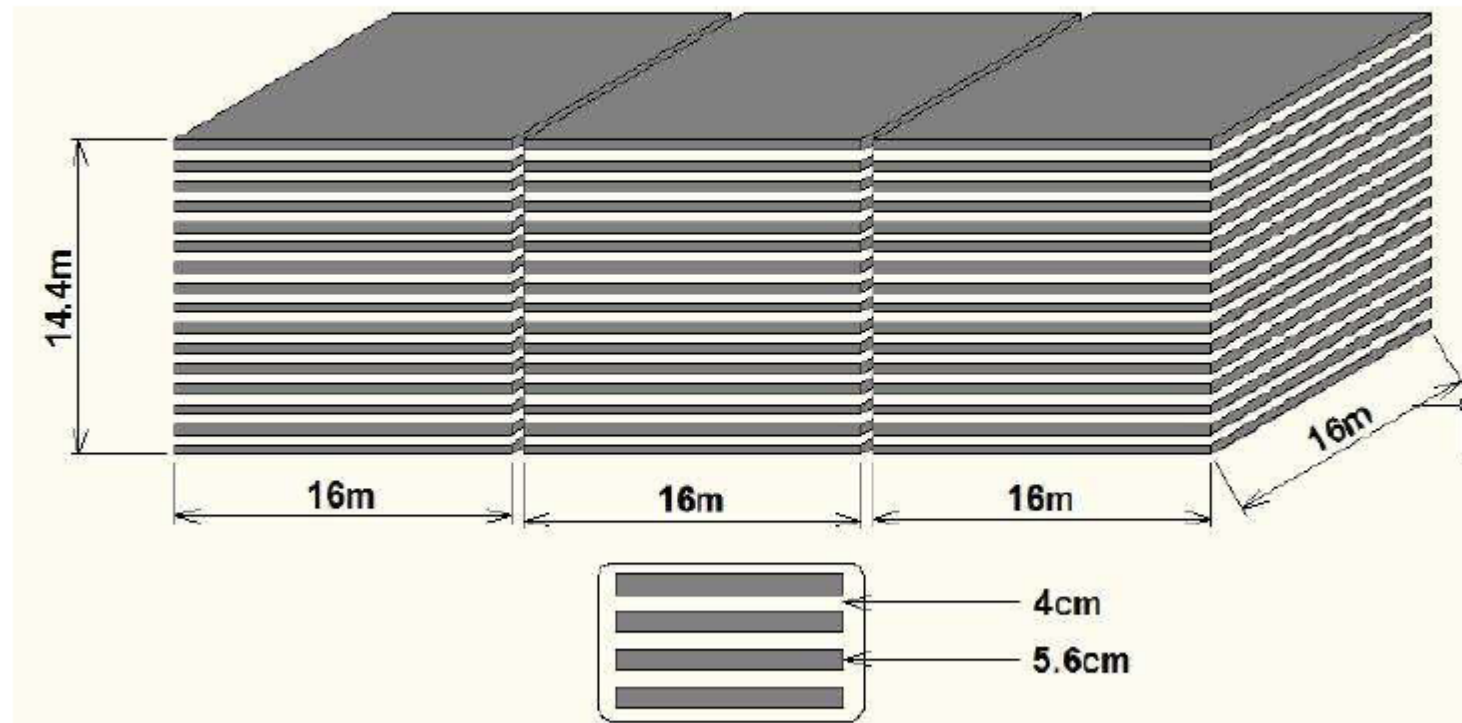


Acknowledgement:

G. Bambhanya, M. Ghosh, P. Ghoshal, C. Gupta, N. Nath, S. Raut

S. Agarwalla, D. Cowen, A. Ghosh, E. Lisi, M. Maltoni, S. Seo, T. Thakur

INO-ICAL Detector



ICAL factsheet

<i>No of modules</i>	<i>3</i>
<i>Module dimension</i>	<i>16 m X 16 m X 14.4m</i>
<i>Detector dimension</i>	<i>48.4 m X 16 m X 14.4m</i>
<i>No of layers</i>	<i>150</i>
<i>Iron plate thickness</i>	<i>5.6cm</i>
<i>Gap for RPC trays</i>	<i>4 cm</i>
<i>Magnetic field</i>	<i>1.4 Tesla</i>
<i>RPC unit dimension</i>	<i>195 cm x 184 cm x 2.4 cm</i>
<i>Readout strip width</i>	<i>3 cm</i>
<i>No. of RPCs/Road/Layer</i>	<i>8</i>
<i>No. of Roads/Layer/Module</i>	<i>8</i>
<i>No. of RPC units/Layer</i>	<i>192</i>
<i>Total no of RPC units</i>	<i>28800</i>
<i>No of Electronic channels</i>	<i>3.7 X 10⁶</i>

Parameter Precision : Future Projections

	Current	e.g JUNO
Δm^2_{12}	$\sim 3\%$	$\sim 0.5\%$
Δm^2_{23}	$\sim 4\%$	$\sim 0.6\%$
$\sin^2\theta_{12}$	$\sim 7\%$	$\sim 0.7\%$
$\sin^2\theta_{23}$	$\sim 15\%$	N/A
$\sin^2\theta_{13}$	$\sim 6\% \rightarrow \sim 4\%$	$\sim 15\%$

L. Wen, talk at Nu2014

H.A. Tanaka, ICHEP 2014

True $\sin^2\theta_{23}$	T2K (5ν)	NO ν A ($3\nu + 3\bar{\nu}$)	T2K + NO ν A
0.36	1.53%	2.33%	1.24% ($2.41^{+0.09}_{-0.09}$)
0.50	1.16%	1.45%	0.87% ($2.41^{+0.07}_{-0.06}$)
0.66	1.53%	2.26%	1.24% ($2.41^{+0.09}_{-0.09}$)

HK

Agarwalla, Prakash, Wang, arXiv:1312.1477 [hep-ph]

True $\sin^2\theta_{23}$	1σ error $\sin^2\theta_{23}$	1σ error Δm^2_{32} (/ 10^{-5} eV 2)
0.45	0.006	1.4
0.50	0.015	1.4
0.55	0.009	1.5